

Mathematica 11.3 Integration Test Results

Test results for the 263 problems in "6.3.7 (d hyper)^m (a+b (c tanh)^n)^p.m"

Problem 7: Result more than twice size of optimal antiderivative.

$$\int \text{Csch}[c + d x]^3 (a + b \text{Tanh}[c + d x]^2) dx$$

Optimal (type 3, 51 leaves, 4 steps):

$$\frac{(a - 2 b) \text{ArcTanh}[\text{Cosh}[c + d x]]}{2 d} - \frac{a \text{Coth}[c + d x] \text{Csch}[c + d x]}{2 d} + \frac{b \text{Sech}[c + d x]}{d}$$

Result (type 3, 123 leaves):

$$\begin{aligned} & -\frac{a \text{Csch}\left[\frac{1}{2}(c + d x)\right]^2}{8 d} + \frac{a \text{Log}\left[\text{Cosh}\left[\frac{1}{2}(c + d x)\right]\right]}{2 d} - \frac{b \text{Log}\left[\text{Cosh}\left[\frac{1}{2}(c + d x)\right]\right]}{d} \\ & - \frac{a \text{Log}\left[\text{Sinh}\left[\frac{1}{2}(c + d x)\right]\right]}{2 d} + \frac{b \text{Log}\left[\text{Sinh}\left[\frac{1}{2}(c + d x)\right]\right]}{d} - \frac{a \text{Sech}\left[\frac{1}{2}(c + d x)\right]^2}{8 d} + \frac{b \text{Sech}[c + d x]}{d} \end{aligned}$$

Problem 26: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sinh}[c + d x]^3}{a + b \text{Tanh}[c + d x]^2} dx$$

Optimal (type 3, 75 leaves, 4 steps):

$$\frac{a \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c + d x]}{\sqrt{a + b}}\right]}{(a + b)^{5/2} d} - \frac{a \text{Cosh}[c + d x]}{(a + b)^2 d} + \frac{\text{Cosh}[c + d x]^3}{3 (a + b) d}$$

Result (type 3, 135 leaves):

$$\begin{aligned} & \frac{1}{12 (a + b)^{5/2} d} \left(12 i a \sqrt{b} \right. \\ & \left. \left(\text{ArcTan}\left[\frac{-i \sqrt{a + b} - \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{b}}\right] + \text{ArcTan}\left[\frac{-i \sqrt{a + b} + \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{b}}\right] \right) - \right. \\ & \left. 3 (3 a - b) \sqrt{a + b} \text{Cosh}[c + d x] + (a + b)^{3/2} \text{Cosh}[3 (c + d x)] \right) \end{aligned}$$

Problem 28: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sinh}[c + d x]}{a + b \text{Tanh}[c + d x]^2} dx$$

Optimal (type 3, 53 leaves, 3 steps):

$$-\frac{\sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c+dx]}{\sqrt{a+b}}\right]}{(a+b)^{3/2} d} + \frac{\text{Cosh}[c + d x]}{(a+b) d}$$

Result (type 3, 107 leaves):

$$\frac{1}{(a+b)^{3/2} d} \left(-i \sqrt{b} \left(\text{ArcTan}\left[\frac{-i \sqrt{a+b} - \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{b}}\right] + \text{ArcTan}\left[\frac{-i \sqrt{a+b} + \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{b}}\right] \right) + \sqrt{a+b} \text{Cosh}[c + d x] \right)$$

Problem 29: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Csch}[c + d x]}{a + b \text{Tanh}[c + d x]^2} dx$$

Optimal (type 3, 55 leaves, 4 steps):

$$-\frac{\text{ArcTanh}[\text{Cosh}[c + d x]]}{a d} + \frac{\sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c+dx]}{\sqrt{a+b}}\right]}{a \sqrt{a+b} d}$$

Result (type 3, 135 leaves):

$$\frac{1}{a d} \left(\frac{i \sqrt{b} \text{ArcTan}\left[\frac{-i \sqrt{a+b} - \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{b}}\right]}{\sqrt{a+b}} + \frac{i \sqrt{b} \text{ArcTan}\left[\frac{-i \sqrt{a+b} + \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{b}}\right]}{\sqrt{a+b}} - \text{Log}\left[\text{Cosh}\left[\frac{1}{2}(c+dx)\right]\right] + \text{Log}\left[\text{Sinh}\left[\frac{1}{2}(c+dx)\right]\right] \right)$$

Problem 31: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Csch}[c + d x]^3}{a + b \text{Tanh}[c + d x]^2} dx$$

Optimal (type 3, 85 leaves, 5 steps):

$$\frac{(a + 2 b) \text{ArcTanh}[\text{Cosh}[c + d x]]}{2 a^2 d} - \frac{\sqrt{b} \sqrt{a + b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c + d x]}{\sqrt{a + b}}\right]}{a^2 d} - \frac{\text{Coth}[c + d x] \text{Csch}[c + d x]}{2 a d}$$

Result (type 3, 198 leaves):

$$\begin{aligned} & -\frac{1}{8 a^2 d} \left(8 i \sqrt{b} \sqrt{a + b} \text{ArcTan}\left[\frac{-i \sqrt{a + b} - \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{b}}\right] + \right. \\ & \quad \left. 8 i \sqrt{b} \sqrt{a + b} \text{ArcTan}\left[\frac{-i \sqrt{a + b} + \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{b}}\right] + \right. \\ & \quad \left. a \text{Csch}\left[\frac{1}{2}(c + d x)\right]^2 - 4 a \text{Log}\left[\text{Cosh}\left[\frac{1}{2}(c + d x)\right]\right] - 8 b \text{Log}\left[\text{Cosh}\left[\frac{1}{2}(c + d x)\right]\right] + \right. \\ & \quad \left. 4 a \text{Log}\left[\text{Sinh}\left[\frac{1}{2}(c + d x)\right]\right] + 8 b \text{Log}\left[\text{Sinh}\left[\frac{1}{2}(c + d x)\right]\right] + a \text{Sech}\left[\frac{1}{2}(c + d x)\right]^2 \right) \end{aligned}$$

Problem 34: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sinh}[c + d x]^3}{(a + b \text{Tanh}[c + d x]^2)^2} dx$$

Optimal (type 3, 124 leaves, 5 steps):

$$\begin{aligned} & \frac{(3 a - 2 b) \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c + d x]}{\sqrt{a + b}}\right]}{2 (a + b)^{7/2} d} - \frac{(a - b) \text{Cosh}[c + d x]}{(a + b)^3 d} + \\ & \frac{\text{Cosh}[c + d x]^3}{3 (a + b)^2 d} + \frac{a b \text{Sech}[c + d x]}{2 (a + b)^3 d (a + b - b \text{Sech}[c + d x]^2)} \end{aligned}$$

Result (type 3, 160 leaves):

$$\begin{aligned} & \frac{1}{12 d} \left(\frac{1}{(a + b)^{7/2}} 6 i (3 a - 2 b) \sqrt{b} \right. \\ & \quad \left. \left(\text{ArcTan}\left[\frac{-i \sqrt{a + b} - \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{b}}\right] + \text{ArcTan}\left[\frac{-i \sqrt{a + b} + \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{b}}\right] \right) \right) + \\ & \frac{3 \text{Cosh}[c + d x] \left(5 b + a \left(-3 + \frac{4 b}{a - b + (a + b) \text{Cosh}[2(c + d x)]} \right) \right)}{(a + b)^3} + \frac{\text{Cosh}[3(c + d x)]}{(a + b)^2} \end{aligned}$$

Problem 36: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sinh}[c + d x]}{(a + b \text{Tanh}[c + d x])^2} dx$$

Optimal (type 3, 92 leaves, 4 steps):

$$-\frac{3 \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c+d x]}{\sqrt{a+b}}\right]}{2 (a+b)^{5/2} d} + \frac{3 \text{Cosh}[c+d x]}{2 (a+b)^2 d} - \frac{\text{Cosh}[c+d x]}{2 (a+b) d (a+b-b \text{Sech}[c+d x]^2)}$$

Result (type 3, 133 leaves):

$$\frac{1}{2 d} \left(-\frac{1}{(a+b)^{5/2}} 3 i \sqrt{b} \left(\text{ArcTan}\left[\frac{-i \sqrt{a+b} - \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{b}}\right] + \text{ArcTan}\left[\frac{-i \sqrt{a+b} + \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c+d x)\right]}{\sqrt{b}}\right] \right) + \frac{2 \text{Cosh}[c+d x] \left(1 - \frac{b}{a-b+(a+b) \text{Cosh}[2(c+d x)]}\right)}{(a+b)^2} \right)$$

Problem 37: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Csch}[c + d x]}{(a + b \text{Tanh}[c + d x])^2} dx$$

Optimal (type 3, 103 leaves, 5 steps):

$$-\frac{\text{ArcTanh}[\text{Cosh}[c + d x]]}{a^2 d} + \frac{\sqrt{b} (3 a + 2 b) \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c+d x]}{\sqrt{a+b}}\right]}{2 a^2 (a+b)^{3/2} d} + \frac{b \text{Sech}[c + d x]}{2 a (a+b) d (a+b-b \text{Sech}[c + d x]^2)}$$

Result (type 3, 188 leaves):

$$\frac{1}{2 a^2 d} \left(\frac{i \sqrt{b} (3 a + 2 b) \operatorname{ArcTan} \left[\frac{-i \sqrt{a+b} - \sqrt{a} \operatorname{Tanh} \left[\frac{1}{2} (c+d x) \right]}{\sqrt{b}} \right]}{(a+b)^{3/2}} + \frac{i \sqrt{b} (3 a + 2 b) \operatorname{ArcTan} \left[\frac{-i \sqrt{a+b} + \sqrt{a} \operatorname{Tanh} \left[\frac{1}{2} (c+d x) \right]}{\sqrt{b}} \right]}{(a+b)^{3/2}} + \frac{2 a b \operatorname{Cosh} [c+d x]}{(a+b) (a-b+(a+b) \operatorname{Cosh} [2(c+d x)])} - 2 \operatorname{Log} \left[\operatorname{Cosh} \left[\frac{1}{2} (c+d x) \right] \right] + 2 \operatorname{Log} \left[\operatorname{Sinh} \left[\frac{1}{2} (c+d x) \right] \right] \right)$$

Problem 39: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csch} [c+d x]^3}{(a+b \operatorname{Tanh} [c+d x]^2)^2} dx$$

Optimal (type 3, 141 leaves, 6 steps):

$$\frac{(a+4 b) \operatorname{ArcTanh} [\operatorname{Cosh} [c+d x]]}{2 a^3 d} - \frac{\sqrt{b} (3 a+4 b) \operatorname{ArcTanh} \left[\frac{\sqrt{b} \operatorname{Sech} [c+d x]}{\sqrt{a+b}} \right]}{2 a^3 \sqrt{a+b} d} - \frac{\operatorname{Coth} [c+d x] \operatorname{Csch} [c+d x]}{2 a d (a+b-b \operatorname{Sech} [c+d x]^2)} - \frac{b \operatorname{Sech} [c+d x]}{a^2 d (a+b-b \operatorname{Sech} [c+d x]^2)}$$

Result (type 3, 314 leaves):

$$\begin{aligned} & -\frac{1}{2 a^3 \sqrt{a+b} d} i \sqrt{b} (3 a+4 b) \operatorname{ArcTan} \left[\frac{1}{\sqrt{b}} \operatorname{Sech} \left[\frac{1}{2} (c+d x) \right] \left(-i \sqrt{a+b} \operatorname{Cosh} \left[\frac{1}{2} (c+d x) \right] - \sqrt{a} \operatorname{Sinh} \left[\frac{1}{2} (c+d x) \right] \right) \right] - \\ & \frac{1}{2 a^3 \sqrt{a+b} d} i \sqrt{b} (3 a+4 b) \operatorname{ArcTan} \left[\frac{1}{\sqrt{b}} \operatorname{Sech} \left[\frac{1}{2} (c+d x) \right] \left(-i \sqrt{a+b} \operatorname{Cosh} \left[\frac{1}{2} (c+d x) \right] + \sqrt{a} \operatorname{Sinh} \left[\frac{1}{2} (c+d x) \right] \right) \right] - \\ & \frac{b \operatorname{Cosh} [c+d x]}{a^2 d (a-b+a \operatorname{Cosh} [2(c+d x)]+b \operatorname{Cosh} [2(c+d x)])} - \frac{\operatorname{Csch} \left[\frac{1}{2} (c+d x) \right]^2}{8 a^2 d} + \\ & \frac{(a+4 b) \operatorname{Log} \left[\operatorname{Cosh} \left[\frac{1}{2} (c+d x) \right] \right]}{2 a^3 d} + \\ & \frac{(-a-4 b) \operatorname{Log} \left[\operatorname{Sinh} \left[\frac{1}{2} (c+d x) \right] \right]}{2 a^3 d} - \frac{\operatorname{Sech} \left[\frac{1}{2} (c+d x) \right]^2}{8 a^2 d} \end{aligned}$$

Problem 42: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sinh}[c + d x]^3}{(a + b \text{Tanh}[c + d x]^2)^3} dx$$

Optimal (type 3, 166 leaves, 6 steps):

$$\frac{5(3a - 4b) \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c + d x]}{\sqrt{a + b}}\right]}{8(a + b)^{9/2} d} - \frac{(a - 2b) \text{Cosh}[c + d x]}{(a + b)^4 d} + \frac{\text{Cosh}[c + d x]^3}{3(a + b)^3 d} +$$

$$\frac{a b \text{Sech}[c + d x]}{4(a + b)^3 d (a + b - b \text{Sech}[c + d x]^2)^2} + \frac{(7a - 4b) b \text{Sech}[c + d x]}{8(a + b)^4 d (a + b - b \text{Sech}[c + d x]^2)}$$

Result (type 3, 227 leaves):

$$\frac{1}{24 d} \left(\frac{1}{(a + b)^{9/2}} 15 i (3a - 4b) \sqrt{b} \right.$$

$$\left. \left(\text{ArcTan}\left[\frac{-i \sqrt{a + b} - \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{b}}\right] + \text{ArcTan}\left[\frac{-i \sqrt{a + b} + \sqrt{a} \text{Tanh}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{b}}\right] \right) - \right.$$

$$\left. \left(6 \text{Cosh}[c + d x] \left(3a^3 - 24a^2 b + 30a b^2 - 13b^3 + (6a^3 - 27a^2 b - 11a b^2 + 22b^3) \text{Cosh}[2(c + d x)] + \right. \right. \right.$$

$$\left. \left. 3(a - 3b)(a + b)^2 \text{Cosh}[2(c + d x)]^2 \right) \right) /$$

$$\left. \left((a + b)^4 (a - b + (a + b) \text{Cosh}[2(c + d x)])^2 + \frac{2 \text{Cosh}[3(c + d x)]}{(a + b)^3} \right) \right)$$

Problem 44: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sinh}[c + d x]}{(a + b \text{Tanh}[c + d x]^2)^3} dx$$

Optimal (type 3, 126 leaves, 5 steps):

$$-\frac{15 \sqrt{b} \text{ArcTanh}\left[\frac{\sqrt{b} \text{Sech}[c + d x]}{\sqrt{a + b}}\right]}{8(a + b)^{7/2} d} + \frac{15 \text{Cosh}[c + d x]}{8(a + b)^3 d} -$$

$$\frac{\text{Cosh}[c + d x]}{4(a + b) d (a + b - b \text{Sech}[c + d x]^2)^2} - \frac{5 \text{Cosh}[c + d x]}{8(a + b)^2 d (a + b - b \text{Sech}[c + d x]^2)}$$

Result (type 3, 157 leaves):

$$\frac{1}{8d} \left(-\frac{1}{(a+b)^{7/2}} 15i\sqrt{b} \right. \\ \left. \left(\operatorname{ArcTan} \left[\frac{-i\sqrt{a+b} - \sqrt{a} \operatorname{Tanh} \left[\frac{1}{2}(c+dx) \right]}{\sqrt{b}} \right] + \operatorname{ArcTan} \left[\frac{-i\sqrt{a+b} + \sqrt{a} \operatorname{Tanh} \left[\frac{1}{2}(c+dx) \right]}{\sqrt{b}} \right] \right) + \right. \\ \left. \frac{2 \operatorname{Cosh}[c+dx] \left(4 - \frac{4b^2}{(a-b+(a+b) \operatorname{Cosh}[2(c+dx)])^2} - \frac{9b}{a-b+(a+b) \operatorname{Cosh}[2(c+dx)]} \right)}{(a+b)^3} \right)$$

Problem 45: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Csch}[c+dx]}{(a+b \operatorname{Tanh}[c+dx]^2)^3} dx$$

Optimal (type 3, 156 leaves, 6 steps):

$$-\frac{\operatorname{ArcTanh}[\operatorname{Cosh}[c+dx]]}{a^3 d} + \frac{\sqrt{b} (15a^2 + 20ab + 8b^2) \operatorname{ArcTanh} \left[\frac{\sqrt{b} \operatorname{Sech}[c+dx]}{\sqrt{a+b}} \right]}{8a^3 (a+b)^{5/2} d} + \\ \frac{b \operatorname{Sech}[c+dx]}{4a(a+b)d(a+b-b \operatorname{Sech}[c+dx]^2)^2} + \frac{b(7a+4b) \operatorname{Sech}[c+dx]}{8a^2(a+b)^2 d(a+b-b \operatorname{Sech}[c+dx]^2)}$$

Result (type 3, 249 leaves):

$$\frac{1}{8a^3 d} \left(\frac{i\sqrt{b} (15a^2 + 20ab + 8b^2) \operatorname{ArcTan} \left[\frac{-i\sqrt{a+b} - \sqrt{a} \operatorname{Tanh} \left[\frac{1}{2}(c+dx) \right]}{\sqrt{b}} \right]}{(a+b)^{5/2}} + \right. \\ \frac{i\sqrt{b} (15a^2 + 20ab + 8b^2) \operatorname{ArcTan} \left[\frac{-i\sqrt{a+b} + \sqrt{a} \operatorname{Tanh} \left[\frac{1}{2}(c+dx) \right]}{\sqrt{b}} \right]}{(a+b)^{5/2}} + \\ \frac{8a^2 b^2 \operatorname{Cosh}[c+dx]}{(a+b)^2 (a-b+(a+b) \operatorname{Cosh}[2(c+dx)])^2} + \frac{2ab(9a+4b) \operatorname{Cosh}[c+dx]}{(a+b)^2 (a-b+(a+b) \operatorname{Cosh}[2(c+dx)])} - \\ \left. 8 \operatorname{Log} \left[\operatorname{Cosh} \left[\frac{1}{2}(c+dx) \right] \right] + 8 \operatorname{Log} \left[\operatorname{Sinh} \left[\frac{1}{2}(c+dx) \right] \right] \right)$$

Problem 47: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Csch}[c+dx]^3}{(a+b \operatorname{Tanh}[c+dx]^2)^3} dx$$

Optimal (type 3, 196 leaves, 7 steps):

$$\frac{(a + 6 b) \operatorname{ArcTanh}[\operatorname{Cosh}[c + d x]]}{2 a^4 d} - \frac{\sqrt{b} (15 a^2 + 40 a b + 24 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Sech}[c + d x]}{\sqrt{a + b}}\right]}{8 a^4 (a + b)^{3/2} d} - \frac{\operatorname{Coth}[c + d x] \operatorname{Csch}[c + d x]}{2 a d (a + b - b \operatorname{Sech}[c + d x]^2)^2} - \frac{3 b \operatorname{Sech}[c + d x]}{4 a^2 d (a + b - b \operatorname{Sech}[c + d x]^2)^2} - \frac{b (11 a + 12 b) \operatorname{Sech}[c + d x]}{8 a^3 (a + b) d (a + b - b \operatorname{Sech}[c + d x]^2)^2}$$

Result (type 3, 401 leaves):

$$\begin{aligned} & - \frac{1}{8 a^4 (a + b)^{3/2} d} \operatorname{ArcTan}\left[\frac{1}{\sqrt{b}} \operatorname{Sech}\left[\frac{1}{2}(c + d x)\right]\right] \left(-i \sqrt{a + b} \operatorname{Cosh}\left[\frac{1}{2}(c + d x)\right] - \sqrt{a} \operatorname{Sinh}\left[\frac{1}{2}(c + d x)\right]\right) - \\ & \frac{1}{8 a^4 (a + b)^{3/2} d} \operatorname{ArcTan}\left[\frac{1}{\sqrt{b}} \operatorname{Sech}\left[\frac{1}{2}(c + d x)\right]\right] \left(-i \sqrt{a + b} \operatorname{Cosh}\left[\frac{1}{2}(c + d x)\right] + \sqrt{a} \operatorname{Sinh}\left[\frac{1}{2}(c + d x)\right]\right) - \\ & \frac{b^2 \operatorname{Cosh}[c + d x]}{a^2 (a + b) d (a - b + a \operatorname{Cosh}[2(c + d x)] + b \operatorname{Cosh}[2(c + d x)])^2} + \\ & \frac{-9 a b \operatorname{Cosh}[c + d x] - 8 b^2 \operatorname{Cosh}[c + d x]}{4 a^3 (a + b) d (a - b + a \operatorname{Cosh}[2(c + d x)] + b \operatorname{Cosh}[2(c + d x)])} - \\ & \frac{\operatorname{Csch}\left[\frac{1}{2}(c + d x)\right]^2}{8 a^3 d} + \frac{(a + 6 b) \operatorname{Log}\left[\operatorname{Cosh}\left[\frac{1}{2}(c + d x)\right]\right]}{2 a^4 d} + \\ & \frac{(-a - 6 b) \operatorname{Log}\left[\operatorname{Sinh}\left[\frac{1}{2}(c + d x)\right]\right]}{2 a^4 d} - \frac{\operatorname{Sech}\left[\frac{1}{2}(c + d x)\right]^2}{8 a^3 d} \end{aligned}$$

Problem 73: Result is not expressed in closed-form.

$$\int \frac{\operatorname{Sinh}[c + d x]^4}{a + b \operatorname{Tanh}[c + d x]^3} dx$$

Optimal (type 3, 491 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{a^{2/3} b^{1/3} (a^2 + 3 a^{4/3} b^{2/3} - b^2) \operatorname{ArcTan}\left[\frac{a^{1/3} - 2 b^{1/3} \operatorname{Tanh}[c+dx]}{\sqrt{3} a^{1/3}}\right]}{\sqrt{3} (a^{4/3} + a^{2/3} b^{2/3} + b^{4/3})^3 d} \\
 & \frac{3 a (a - 5 b) \operatorname{Log}[1 - \operatorname{Tanh}[c + dx]]}{16 (a + b)^3 d} + \frac{3 a (a + 5 b) \operatorname{Log}[1 + \operatorname{Tanh}[c + dx]]}{16 (a - b)^3 d} - \frac{1}{3 (a^2 - b^2)^3 d} \\
 & a^{2/3} b^{1/3} (a^4 + 7 a^2 b^2 + b^4 + 3 a^{2/3} b^{4/3} (2 a^2 + b^2)) \operatorname{Log}[a^{1/3} + b^{1/3} \operatorname{Tanh}[c + dx]] + \frac{1}{6 (a^2 - b^2)^3 d} a^{2/3} \\
 & b^{1/3} (a^4 + 7 a^2 b^2 + b^4 + 3 a^{2/3} b^{4/3} (2 a^2 + b^2)) \operatorname{Log}[a^{2/3} - a^{1/3} b^{1/3} \operatorname{Tanh}[c + dx] + b^{2/3} \operatorname{Tanh}[c + dx]^2] - \\
 & \frac{a^2 b (a^2 + 2 b^2) \operatorname{Log}[a + b \operatorname{Tanh}[c + dx]^3]}{(a^2 - b^2)^3 d} + \frac{1}{16 (a + b) d (1 - \operatorname{Tanh}[c + dx])^2} - \\
 & \frac{5 a - b}{16 (a + b)^2 d (1 - \operatorname{Tanh}[c + dx])} - \frac{1}{16 (a - b) d (1 + \operatorname{Tanh}[c + dx])^2} + \frac{5 a + b}{16 (a - b)^2 d (1 + \operatorname{Tanh}[c + dx])}
 \end{aligned}$$

Result (type 7, 645 leaves):

$$\begin{aligned}
 & \frac{1}{96 (a - b)^2 (a + b)^3 d} \left(-32 a b \operatorname{RootSum}\left[\right. \right. \\
 & \quad a - b + 3 a \#1 + 3 b \#1 + 3 a \#1^2 - 3 b \#1^2 + a \#1^3 + b \#1^3 \&, \frac{1}{a - b + 2 a \#1 + 2 b \#1 + a \#1^2 - b \#1^2} \\
 & \quad \left(-6 a^3 c - 12 a b^2 c - 6 a^3 d x - 12 a b^2 d x + 3 a^3 \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] + 6 a b^2 \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] - \right. \\
 & \quad 8 a^3 c \#1 + 4 a^2 b c \#1 + 8 a b^2 c \#1 - 4 b^3 c \#1 - 8 a^3 d x \#1 + 4 a^2 b d x \#1 + \\
 & \quad 8 a b^2 d x \#1 - 4 b^3 d x \#1 + 4 a^3 \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] \#1 - 2 a^2 b \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] \#1 - \\
 & \quad 4 a b^2 \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] \#1 + 2 b^3 \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] \#1 - 10 a^3 c \#1^2 + 20 a^2 b c \#1^2 - \\
 & \quad 20 a b^2 c \#1^2 + 4 b^3 c \#1^2 - 10 a^3 d x \#1^2 + 20 a^2 b d x \#1^2 - 20 a b^2 d x \#1^2 + \\
 & \quad 4 b^3 d x \#1^2 + 5 a^3 \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] \#1^2 - 10 a^2 b \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] \#1^2 + \\
 & \quad \left. \left. 10 a b^2 \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] \#1^2 - 2 b^3 \operatorname{Log}\left[e^{2(c+dx)} - \#1 \right] \#1^2 \right) \& \right] + \\
 & \quad 3 \left(4 b (5 a^3 + 5 a^2 b + a b^2 + b^3) \operatorname{Cosh}[2(c + dx)] - (a - b) b (a + b)^2 \operatorname{Cosh}[4(c + dx)] - \right. \\
 & \quad \left. 8 a (a^3 + a^2 b + 2 a b^2 + 2 b^3) \operatorname{Sinh}[2(c + dx)] + \right. \\
 & \quad \left. a (a - b) \left(12 (a^2 - 6 a b + 5 b^2) (c + dx) + (a + b)^2 \operatorname{Sinh}[4(c + dx)] \right) \right) \right)
 \end{aligned}$$

Problem 75: Result is not expressed in closed-form.

$$\int \frac{\operatorname{Sinh}[c + dx]^2}{a + b \operatorname{Tanh}[c + dx]^3} dx$$

Optimal (type 3, 384 leaves, 11 steps):

$$\frac{a^{2/3} b^{1/3} (a^2 - 3 a^{2/3} b^{4/3} + 2 b^2) \operatorname{ArcTan}\left[\frac{a^{1/3} - 2 b^{1/3} \operatorname{Tanh}[c + d x]}{\sqrt{3} a^{1/3}}\right]}{\sqrt{3} (a^2 - b^2)^2 d} + \frac{(a - 2 b) \operatorname{Log}[1 - \operatorname{Tanh}[c + d x]]}{4 (a + b)^2 d} -$$

$$\frac{(a + 2 b) \operatorname{Log}[1 + \operatorname{Tanh}[c + d x]]}{4 (a - b)^2 d} + \frac{a^{2/3} b^{1/3} (a^2 + 3 a^{2/3} b^{4/3} + 2 b^2) \operatorname{Log}[a^{1/3} + b^{1/3} \operatorname{Tanh}[c + d x]]}{3 (a^2 - b^2)^2 d} -$$

$$\frac{1}{6 (a^2 - b^2)^2 d} a^{2/3} b^{1/3} (a^2 + 3 a^{2/3} b^{4/3} + 2 b^2) \operatorname{Log}[a^{2/3} - a^{1/3} b^{1/3} \operatorname{Tanh}[c + d x] + b^{2/3} \operatorname{Tanh}[c + d x]^2] +$$

$$\frac{b (2 a^2 + b^2) \operatorname{Log}[a + b \operatorname{Tanh}[c + d x]^3]}{3 (a^2 - b^2)^2 d} +$$

$$\frac{1}{4 (a + b) d (1 - \operatorname{Tanh}[c + d x])} - \frac{1}{4 (a - b) d (1 + \operatorname{Tanh}[c + d x])}$$

Result (type 7, 423 leaves):

$$- \frac{1}{12 (a - b) (a + b)^2 d} \left(6 (a^2 - 3 a b + 2 b^2) (c + d x) + 3 b (a + b) \operatorname{Cosh}[2 (c + d x)] + \right.$$

$$4 b \operatorname{RootSum}\left[a - b + 3 a \#1 + 3 b \#1 + 3 a \#1^2 - 3 b \#1^2 + a \#1^3 + b \#1^3 \&, \right.$$

$$\left. \frac{1}{a - b + 2 a \#1 + 2 b \#1 + a \#1^2 - b \#1^2} \left(4 a^2 c + 2 b^2 c + 4 a^2 d x + 2 b^2 d x - 2 a^2 \operatorname{Log}\left[e^{2 (c + d x)} - \#1 \right] - \right.$$

$$b^2 \operatorname{Log}\left[e^{2 (c + d x)} - \#1 \right] + 4 a^2 c \#1 - 4 b^2 c \#1 + 4 a^2 d x \#1 - 4 b^2 d x \#1 -$$

$$2 a^2 \operatorname{Log}\left[e^{2 (c + d x)} - \#1 \right] \#1 + 2 b^2 \operatorname{Log}\left[e^{2 (c + d x)} - \#1 \right] \#1 + 8 a^2 c \#1^2 - 8 a b c \#1^2 +$$

$$2 b^2 c \#1^2 + 8 a^2 d x \#1^2 - 8 a b d x \#1^2 + 2 b^2 d x \#1^2 - 4 a^2 \operatorname{Log}\left[e^{2 (c + d x)} - \#1 \right] \#1^2 +$$

$$\left. \left. 4 a b \operatorname{Log}\left[e^{2 (c + d x)} - \#1 \right] \#1^2 - b^2 \operatorname{Log}\left[e^{2 (c + d x)} - \#1 \right] \#1^2 \right) \& \right] - 3 a (a + b) \operatorname{Sinh}[2 (c + d x)] \left. \right)$$

Problem 78: Result is not expressed in closed-form.

$$\int \frac{\operatorname{Csch}[c + d x]^2}{a + b \operatorname{Tanh}[c + d x]^3} dx$$

Optimal (type 3, 157 leaves, 8 steps):

$$\frac{b^{1/3} \operatorname{ArcTan}\left[\frac{a^{1/3} - 2 b^{1/3} \operatorname{Tanh}[c + d x]}{\sqrt{3} a^{1/3}}\right]}{\sqrt{3} a^{4/3} d} - \frac{\operatorname{Coth}[c + d x]}{a d} + \frac{b^{1/3} \operatorname{Log}[a^{1/3} + b^{1/3} \operatorname{Tanh}[c + d x]]}{3 a^{4/3} d} -$$

$$\frac{b^{1/3} \operatorname{Log}[a^{2/3} - a^{1/3} b^{1/3} \operatorname{Tanh}[c + d x] + b^{2/3} \operatorname{Tanh}[c + d x]^2]}{6 a^{4/3} d}$$

Result (type 7, 190 leaves):

$$- \frac{1}{3 a d} \left(3 \operatorname{Coth}[c + d x] + 2 b \operatorname{RootSum}\left[a - b + 3 a \#1 + 3 b \#1 + 3 a \#1^2 - 3 b \#1^2 + a \#1^3 + b \#1^3 \&, \right.$$

$$\left. \left(-c - d x - \operatorname{Log}[-\operatorname{Cosh}[c + d x] - \operatorname{Sinh}[c + d x]] + \operatorname{Cosh}[c + d x] \#1 - \operatorname{Sinh}[c + d x] \#1 + c \#1 + \right. \right.$$

$$d x \#1 + \operatorname{Log}[-\operatorname{Cosh}[c + d x] - \operatorname{Sinh}[c + d x]] + \operatorname{Cosh}[c + d x] \#1 - \operatorname{Sinh}[c + d x] \#1 \#1 \left. \right) /$$

$$\left. \left(a + b + 2 a \#1 - 2 b \#1 + a \#1^2 + b \#1^2 \right) \& \right]$$

Problem 80: Result is not expressed in closed-form.

$$\int \frac{\text{Csch}[c + d x]^4}{a + b \text{Tanh}[c + d x]^3} dx$$

Optimal (type 3, 215 leaves, 12 steps):

$$\begin{aligned} & -\frac{b^{1/3} \text{ArcTan}\left[\frac{a^{1/3}-2b^{1/3}\text{Tanh}[c+dx]}{\sqrt{3}a^{1/3}}\right]}{\sqrt{3}a^{4/3}d} + \frac{\text{Coth}[c+dx]}{ad} - \\ & \frac{\text{Coth}[c+dx]^3}{3ad} - \frac{b \text{Log}[\text{Tanh}[c+dx]]}{a^2d} - \frac{b^{1/3} \text{Log}[a^{1/3} + b^{1/3} \text{Tanh}[c+dx]]}{3a^{4/3}d} + \\ & \frac{b^{1/3} \text{Log}[a^{2/3} - a^{1/3} b^{1/3} \text{Tanh}[c+dx] + b^{2/3} \text{Tanh}[c+dx]^2]}{6a^{4/3}d} + \frac{b \text{Log}[a + b \text{Tanh}[c+dx]^3]}{3a^2d} \end{aligned}$$

Result (type 7, 322 leaves):

$$\begin{aligned} & \frac{1}{3a^2d} \left(-a \text{Coth}[c+dx] \left(-2 + \text{Csch}[c+dx]^2 \right) + 3b \left(c+dx - \text{Log}[\text{Sinh}[c+dx]] \right) \right) + \\ & b \text{RootSum}\left[a - b + 3a\#1 + 3b\#1 + 3a\#1^2 - 3b\#1^2 + a\#1^3 + b\#1^3 \&, \right. \\ & \quad \left(-2ac + 2bc - 2adx + 2bdx + a \text{Log}[e^{2(c+dx)} - \#1] - b \text{Log}[e^{2(c+dx)} - \#1] - 8ac\#1 - \right. \\ & \quad \left. 4bc\#1 - 8adx\#1 - 4bdx\#1 + 4a \text{Log}[e^{2(c+dx)} - \#1]\#1 + 2b \text{Log}[e^{2(c+dx)} - \#1]\#1 + \right. \\ & \quad \left. 2ac\#1^2 + 2bc\#1^2 + 2adx\#1^2 + 2bdx\#1^2 - a \text{Log}[e^{2(c+dx)} - \#1]\#1^2 - \right. \\ & \quad \left. b \text{Log}[e^{2(c+dx)} - \#1]\#1^2 \right) / \left(a - b + 2a\#1 + 2b\#1 + a\#1^2 - b\#1^2 \& \right) \end{aligned}$$

Problem 104: Result more than twice size of optimal antiderivative.

$$\int \text{Sech}[c + d x]^4 (a + b \text{Tanh}[c + d x]^2)^3 dx$$

Optimal (type 3, 102 leaves, 3 steps):

$$\begin{aligned} & \frac{a^3 \text{Tanh}[c+dx]}{d} - \frac{a^2(a-3b) \text{Tanh}[c+dx]^3}{3d} - \\ & \frac{3a(a-b)b \text{Tanh}[c+dx]^5}{5d} - \frac{(3a-b)b^2 \text{Tanh}[c+dx]^7}{7d} - \frac{b^3 \text{Tanh}[c+dx]^9}{9d} \end{aligned}$$

Result (type 3, 218 leaves):

$$\begin{aligned} & \frac{1}{20160d} \\ & \left(5775a^3 - 1071a^2b + 621ab^2 - 725b^3 + 10(903a^3 - 63a^2b - 27ab^2 + 107b^3) \text{Cosh}[2(c+dx)] \right) + \\ & 8(525a^3 + 126a^2b - 81ab^2 - 50b^3) \text{Cosh}[4(c+dx)] + \\ & 1050a^3 \text{Cosh}[6(c+dx)] + 630a^2b \text{Cosh}[6(c+dx)] + 270ab^2 \text{Cosh}[6(c+dx)] + \\ & 50b^3 \text{Cosh}[6(c+dx)] + 105a^3 \text{Cosh}[8(c+dx)] + 63a^2b \text{Cosh}[8(c+dx)] + \\ & 27ab^2 \text{Cosh}[8(c+dx)] + 5b^3 \text{Cosh}[8(c+dx)] \text{Sech}[c+dx]^8 \text{Tanh}[c+dx] \end{aligned}$$

Problem 133: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Sech}[c + d x]^7}{(a + b \text{Tanh}[c + d x]^2)^3} dx$$

Optimal (type 3, 156 leaves, 6 steps):

$$-\frac{\text{ArcTan}[\text{Sinh}[c + d x]]}{b^3 d} + \frac{\sqrt{a + b} (8 a^2 - 4 a b + 3 b^2) \text{ArcTan}\left[\frac{\sqrt{a + b} \text{Sinh}[c + d x]}{\sqrt{a}}\right]}{8 a^{5/2} b^3 d} + \frac{(a + b) \text{Sinh}[c + d x]}{4 a b d (a + (a + b) \text{Sinh}[c + d x]^2)^2} - \frac{(4 a - 3 b) (a + b) \text{Sinh}[c + d x]}{8 a^2 b^2 d (a + (a + b) \text{Sinh}[c + d x]^2)}$$

Result (type 3, 317 leaves):

$$-\frac{1}{32 b^3 d} \left(\frac{2 \sqrt{a + b} (8 a^2 - 4 a b + 3 b^2) \text{ArcTan}\left[\frac{\sqrt{a} \text{Csch}[c + d x]}{\sqrt{a + b}}\right]}{a^{5/2}} + \frac{2 (8 a^3 + 4 a^2 b - a b^2 + 3 b^3) \text{ArcTan}\left[\frac{\sqrt{a} \text{Csch}[c + d x]}{\sqrt{a + b}}\right]}{a^{5/2} \sqrt{a + b}} + 64 \text{ArcTan}\left[\text{Tanh}\left[\frac{1}{2} (c + d x)\right]\right] + \frac{i \sqrt{a + b} (8 a^2 - 4 a b + 3 b^2) \text{Log}[a - b + (a + b) \text{Cosh}[2 (c + d x)]]}{a^{5/2}} - \frac{i (8 a^3 + 4 a^2 b - a b^2 + 3 b^3) \text{Log}[a - b + (a + b) \text{Cosh}[2 (c + d x)]]}{a^{5/2} \sqrt{a + b}} + \frac{32 b^2 (a + b) \text{Sinh}[c + d x]}{a (a - b + (a + b) \text{Cosh}[2 (c + d x)])^2} + \frac{8 b (4 a^2 + a b - 3 b^2) \text{Sinh}[c + d x]}{a^2 (a - b + (a + b) \text{Cosh}[2 (c + d x)])} \right)$$

Problem 144: Result more than twice size of optimal antiderivative.

$$\int \text{Tanh}[c + d x]^4 (a + b \text{Tanh}[c + d x]^2)^2 dx$$

Optimal (type 3, 83 leaves, 4 steps):

$$(a + b)^2 x - \frac{(a + b)^2 \text{Tanh}[c + d x]}{d} - \frac{(a + b)^2 \text{Tanh}[c + d x]^3}{3 d} - \frac{b (2 a + b) \text{Tanh}[c + d x]^5}{5 d} - \frac{b^2 \text{Tanh}[c + d x]^7}{7 d}$$

Result (type 3, 205 leaves):

$$\begin{aligned}
 & a^2 x + 2 a b x + b^2 x - \frac{4 a^2 \operatorname{Tanh}[c+d x]}{3 d} - \frac{46 a b \operatorname{Tanh}[c+d x]}{15 d} - \frac{176 b^2 \operatorname{Tanh}[c+d x]}{105 d} + \\
 & \frac{a^2 \operatorname{Sech}[c+d x]^2 \operatorname{Tanh}[c+d x]}{3 d} + \frac{22 a b \operatorname{Sech}[c+d x]^2 \operatorname{Tanh}[c+d x]}{15 d} + \\
 & \frac{122 b^2 \operatorname{Sech}[c+d x]^2 \operatorname{Tanh}[c+d x]}{105 d} - \frac{2 a b \operatorname{Sech}[c+d x]^4 \operatorname{Tanh}[c+d x]}{5 d} - \\
 & \frac{22 b^2 \operatorname{Sech}[c+d x]^4 \operatorname{Tanh}[c+d x]}{35 d} + \frac{b^2 \operatorname{Sech}[c+d x]^6 \operatorname{Tanh}[c+d x]}{7 d}
 \end{aligned}$$

Problem 146: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Tanh}[c+d x]^2 (a+b \operatorname{Tanh}[c+d x]^2)^2 dx$$

Optimal (type 3, 63 leaves, 4 steps):

$$(a+b)^2 x - \frac{(a+b)^2 \operatorname{Tanh}[c+d x]}{d} - \frac{b(2a+b) \operatorname{Tanh}[c+d x]^3}{3 d} - \frac{b^2 \operatorname{Tanh}[c+d x]^5}{5 d}$$

Result (type 3, 132 leaves):

$$\begin{aligned}
 & a^2 x + 2 a b x + b^2 x - \frac{a^2 \operatorname{Tanh}[c+d x]}{d} - \frac{8 a b \operatorname{Tanh}[c+d x]}{3 d} - \\
 & \frac{23 b^2 \operatorname{Tanh}[c+d x]}{15 d} + \frac{2 a b \operatorname{Sech}[c+d x]^2 \operatorname{Tanh}[c+d x]}{3 d} + \\
 & \frac{11 b^2 \operatorname{Sech}[c+d x]^2 \operatorname{Tanh}[c+d x]}{15 d} - \frac{b^2 \operatorname{Sech}[c+d x]^4 \operatorname{Tanh}[c+d x]}{5 d}
 \end{aligned}$$

Problem 154: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Coth}[c+d x]^6 (a+b \operatorname{Tanh}[c+d x]^2)^2 dx$$

Optimal (type 3, 63 leaves, 4 steps):

$$(a+b)^2 x - \frac{(a+b)^2 \operatorname{Coth}[c+d x]}{d} - \frac{a(a+2b) \operatorname{Coth}[c+d x]^3}{3 d} - \frac{a^2 \operatorname{Coth}[c+d x]^5}{5 d}$$

Result (type 3, 132 leaves):

$$\begin{aligned}
 & a^2 x + 2 a b x + b^2 x - \frac{23 a^2 \operatorname{Coth}[c+d x]}{15 d} - \frac{8 a b \operatorname{Coth}[c+d x]}{3 d} - \\
 & \frac{b^2 \operatorname{Coth}[c+d x]}{d} - \frac{11 a^2 \operatorname{Coth}[c+d x] \operatorname{Csch}[c+d x]^2}{15 d} - \\
 & \frac{2 a b \operatorname{Coth}[c+d x] \operatorname{Csch}[c+d x]^2}{3 d} - \frac{a^2 \operatorname{Coth}[c+d x] \operatorname{Csch}[c+d x]^4}{5 d}
 \end{aligned}$$

Problem 156: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Tanh}[c + d x]^4 (a + b \operatorname{Tanh}[c + d x]^2)^3 dx$$

Optimal (type 3, 114 leaves, 4 steps):

$$(a + b)^3 x - \frac{(a + b)^3 \operatorname{Tanh}[c + d x]}{d} - \frac{(a + b)^3 \operatorname{Tanh}[c + d x]^3}{3 d} - \frac{b (3 a^2 + 3 a b + b^2) \operatorname{Tanh}[c + d x]^5}{5 d} - \frac{b^2 (3 a + b) \operatorname{Tanh}[c + d x]^7}{7 d} - \frac{b^3 \operatorname{Tanh}[c + d x]^9}{9 d}$$

Result (type 3, 640 leaves):

$$\frac{1}{80640 d} \operatorname{Sech}[c + d x]^9 (39690 a^3 (c + d x) \operatorname{Cosh}[c + d x] + 119070 a^2 b (c + d x) \operatorname{Cosh}[c + d x] + 119070 a b^2 (c + d x) \operatorname{Cosh}[c + d x] + 39690 b^3 (c + d x) \operatorname{Cosh}[c + d x] + 26460 a^3 (c + d x) \operatorname{Cosh}[3 (c + d x)] + 79380 a^2 b (c + d x) \operatorname{Cosh}[3 (c + d x)] + 79380 a b^2 (c + d x) \operatorname{Cosh}[3 (c + d x)] + 26460 b^3 (c + d x) \operatorname{Cosh}[3 (c + d x)] + 11340 a^3 (c + d x) \operatorname{Cosh}[5 (c + d x)] + 34020 a^2 b (c + d x) \operatorname{Cosh}[5 (c + d x)] + 34020 a b^2 (c + d x) \operatorname{Cosh}[5 (c + d x)] + 11340 b^3 (c + d x) \operatorname{Cosh}[5 (c + d x)] + 2835 a^3 (c + d x) \operatorname{Cosh}[7 (c + d x)] + 8505 a^2 b (c + d x) \operatorname{Cosh}[7 (c + d x)] + 8505 a b^2 (c + d x) \operatorname{Cosh}[7 (c + d x)] + 2835 b^3 (c + d x) \operatorname{Cosh}[7 (c + d x)] + 315 a^3 (c + d x) \operatorname{Cosh}[9 (c + d x)] + 945 a^2 b (c + d x) \operatorname{Cosh}[9 (c + d x)] + 945 a b^2 (c + d x) \operatorname{Cosh}[9 (c + d x)] + 315 b^3 (c + d x) \operatorname{Cosh}[9 (c + d x)] - 3780 a^3 \operatorname{Sinh}[c + d x] - 12474 a^2 b \operatorname{Sinh}[c + d x] - 10584 a b^2 \operatorname{Sinh}[c + d x] - 7938 b^3 \operatorname{Sinh}[c + d x] - 7980 a^3 \operatorname{Sinh}[3 (c + d x)] - 24696 a^2 b \operatorname{Sinh}[3 (c + d x)] - 24696 a b^2 \operatorname{Sinh}[3 (c + d x)] - 5292 b^3 \operatorname{Sinh}[3 (c + d x)] - 6300 a^3 \operatorname{Sinh}[5 (c + d x)] - 18144 a^2 b \operatorname{Sinh}[5 (c + d x)] - 19224 a b^2 \operatorname{Sinh}[5 (c + d x)] - 7668 b^3 \operatorname{Sinh}[5 (c + d x)] - 2520 a^3 \operatorname{Sinh}[7 (c + d x)] - 7371 a^2 b \operatorname{Sinh}[7 (c + d x)] - 6696 a b^2 \operatorname{Sinh}[7 (c + d x)] - 1917 b^3 \operatorname{Sinh}[7 (c + d x)] - 420 a^3 \operatorname{Sinh}[9 (c + d x)] - 1449 a^2 b \operatorname{Sinh}[9 (c + d x)] - 1584 a b^2 \operatorname{Sinh}[9 (c + d x)] - 563 b^3 \operatorname{Sinh}[9 (c + d x)])$$

Problem 202: Result more than twice size of optimal antiderivative.

$$\int \sqrt{1 - \operatorname{Tanh}[x]^2} dx$$

Optimal (type 3, 3 leaves, 3 steps):

$$\operatorname{ArcSin}[\operatorname{Tanh}[x]]$$

Result (type 3, 19 leaves):

$$2 \operatorname{ArcTan}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]\right] \operatorname{Cosh}[x] \sqrt{\operatorname{Sech}[x]^2}$$

Problem 208: Result more than twice size of optimal antiderivative.

$$\int \text{Tanh}[x]^5 \sqrt{a + b \text{Tanh}[x]^2} \, dx$$

Optimal (type 3, 87 leaves, 7 steps):

$$\sqrt{a+b} \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a+b}}\right] - \sqrt{a+b \text{Tanh}[x]^2} + \frac{(a-b)(a+b \text{Tanh}[x]^2)^{3/2}}{3b^2} - \frac{(a+b \text{Tanh}[x]^2)^{5/2}}{5b^2}$$

Result (type 3, 184 leaves):

$$\frac{1}{15\sqrt{2}} \sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}[x]^2} \left(-23 + \frac{2a^2}{b^2} - \frac{6a}{b} - \left(15\sqrt{2} \sqrt{a+b} \text{Cosh}[x] \left(\text{Log}\left[-\text{Sech}\left[\frac{x}{2}\right]^2\right] - \text{Log}\left[a + b + \frac{\sqrt{a+b} \sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a+b) \text{Tanh}\left[\frac{x}{2}\right]^2 \right] \text{Sech}\left[\frac{x}{2}\right]^2 \right) \right) \right) / \left(\sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4} \right) + \left(11 + \frac{a}{b} \right) \text{Sech}[x]^2 - 3 \text{Sech}[x]^4$$

Problem 209: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \text{Tanh}[x]^4 \sqrt{a + b \text{Tanh}[x]^2} \, dx$$

Optimal (type 3, 121 leaves, 8 steps):

$$\frac{(a^2 - 4ab - 8b^2) \text{ArcTanh}\left[\frac{\sqrt{b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{8b^{3/2}} + \sqrt{a+b} \text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right] - \frac{(a+4b) \text{Tanh}[x] \sqrt{a+b \text{Tanh}[x]^2}}{8b} - \frac{1}{4} \text{Tanh}[x]^3 \sqrt{a+b \text{Tanh}[x]^2}$$

Result (type 4, 580 leaves):

$$\begin{aligned}
 & \frac{1}{4b} \left(- \left(\left(b (a^2 - 4b^2) \sqrt{\frac{a - b + (a + b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \sqrt{-\frac{a \operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right. \right. \right. \\
 & \quad \left. \sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \operatorname{Csch}[2x] \operatorname{EllipticF} \left[\right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin} \left[\frac{\sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}} \right], 1 \right] \operatorname{Sinh}[x]^4 \right) / (a (a - b + (a + b) \operatorname{Cosh}[2x])) \right) - \\
 & \frac{1}{\sqrt{a - b + (a + b) \operatorname{Cosh}[2x]}} 4 i b (4 a b + 4 b^2) \sqrt{1 + \operatorname{Cosh}[2x]} \sqrt{\frac{a - b + (a + b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \\
 & \left(- \left(\left(i \sqrt{-\frac{a \operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right. \right. \right. \\
 & \quad \left. \sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \operatorname{Csch}[2x] \right. \\
 & \quad \left. \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}} \right], 1 \right] \operatorname{Sinh}[x]^4 \right) / \\
 & \quad \left. \left(4 a \sqrt{1 + \operatorname{Cosh}[2x]} \sqrt{a - b + (a + b) \operatorname{Cosh}[2x]} \right) \right) + \\
 & \left(i \sqrt{-\frac{a \operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Csch}[2x] \text{EllipticPi}\left[\frac{b}{a+b}, \text{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\text{Cosh}[2x])\text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \text{Sinh}[x]^4 \right) / \\
 & \left. \left(2(a+b) \sqrt{1+\text{Cosh}[2x]} \sqrt{a-b+(a+b)\text{Cosh}[2x]} \right) \right) + \\
 & \sqrt{\frac{a-b+a\text{Cosh}[2x]+b\text{Cosh}[2x]}{1+\text{Cosh}[2x]}} \left(\frac{\text{Sech}[x](-a\text{Sinh}[x]-6b\text{Sinh}[x])}{8b} + \right. \\
 & \left. \frac{1}{4} \text{Sech}[x]^2 \right. \\
 & \left. \text{Tanh}[x] \right)
 \end{aligned}$$

Problem 210: Result more than twice size of optimal antiderivative.

$$\int \text{Tanh}[x]^3 \sqrt{a+b\text{Tanh}[x]^2} \, dx$$

Optimal (type 3, 63 leaves, 6 steps):

$$\sqrt{a+b} \text{ArcTanh}\left[\frac{\sqrt{a+b\text{Tanh}[x]^2}}{\sqrt{a+b}}\right] - \sqrt{a+b\text{Tanh}[x]^2} - \frac{(a+b\text{Tanh}[x]^2)^{3/2}}{3b}$$

Result (type 3, 310 leaves):

$$\sqrt{\frac{a - b + a \operatorname{Cosh}[2x] + b \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \left(-\frac{a + 4b}{3b} + \frac{\operatorname{Sech}[x]^2}{3} \right) +$$

$$\left(\sqrt{a+b} (1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2x]}{(1 + \operatorname{Cosh}[x])^2}} \sqrt{\frac{a - b + (a+b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \left(\operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] - \right.$$

$$\left. \operatorname{Log}\left[a + b + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a+b} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right] \right)$$

$$\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) /$$

$$\left(\sqrt{a - b + (a+b) \operatorname{Cosh}[2x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right)$$

Problem 211: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Tanh}[x]^2 \sqrt{a + b \operatorname{Tanh}[x]^2} dx$$

Optimal (type 3, 85 leaves, 7 steps):

$$\frac{(a + 2b) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^2}}\right]}{2\sqrt{b}} + \sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^2}}\right] - \frac{1}{2} \operatorname{Tanh}[x] \sqrt{a+b \operatorname{Tanh}[x]^2}$$

Result (type 4, 531 leaves):

$$\left(b^2 \sqrt{\frac{a - b + (a+b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \sqrt{\frac{a \operatorname{Coth}[x]^2}{b}} \right.$$

$$\sqrt{\frac{a (1 + \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \sqrt{\frac{(a - b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}$$

$$\left. \operatorname{Csch}[2x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}}{b}\right], 1\right] \operatorname{Sinh}[x]^4 \right) /$$

$$(a (a - b + (a+b) \operatorname{Cosh}[2x])) - \frac{1}{\sqrt{a - b + (a+b) \operatorname{Cosh}[2x]}}$$

$$\begin{aligned}
 & 4 \, i \, b \, (a + b) \sqrt{1 + \text{Cosh}[2x]} \sqrt{\frac{a - b + (a + b) \text{Cosh}[2x]}{1 + \text{Cosh}[2x]}} \\
 & \left(- \left(\left(\left(i \sqrt{-\frac{a \text{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \sqrt{\frac{(a - b + (a + b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Csch}[2x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(a - b + (a + b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \text{Sinh}[x]^4 \right) / \right. \right. \\
 & \quad \left. \left. \left(4 a \sqrt{1 + \text{Cosh}[2x]} \sqrt{a - b + (a + b) \text{Cosh}[2x]} \right) \right) + \right. \\
 & \left. \left(i \sqrt{-\frac{a \text{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \sqrt{\frac{(a - b + (a + b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \right. \right. \\
 & \quad \left. \left. \text{Csch}[2x] \text{EllipticPi}\left[\frac{b}{a + b}, \text{ArcSin}\left[\frac{\sqrt{\frac{(a - b + (a + b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \text{Sinh}[x]^4 \right) / \right. \\
 & \quad \left. \left(2 (a + b) \sqrt{1 + \text{Cosh}[2x]} \sqrt{a - b + (a + b) \text{Cosh}[2x]} \right) \right) - \\
 & \frac{1}{2} \sqrt{\frac{a - b + a \text{Cosh}[2x] + b \text{Cosh}[2x]}{1 + \text{Cosh}[2x]}} \text{Tanh}[x]
 \end{aligned}$$

Problem 212: Result more than twice size of optimal antiderivative.

$$\int \text{Tanh}[x] \sqrt{a + b \text{Tanh}[x]^2} \, dx$$

Optimal (type 3, 44 leaves, 5 steps):

$$\sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right] - \sqrt{a+b \operatorname{Tanh}[x]^2}$$

Result (type 3, 214 leaves):

$$- \left(\left(\left(\sqrt{\frac{a-b+a \operatorname{Cosh}[2x]+b \operatorname{Cosh}[2x]}{3+4 \operatorname{Cosh}[x]+\operatorname{Cosh}[2x]}} + \operatorname{Cosh}[x] \left(\sqrt{\frac{a-b+a \operatorname{Cosh}[2x]+b \operatorname{Cosh}[2x]}{3+4 \operatorname{Cosh}[x]+\operatorname{Cosh}[2x]}} + \sqrt{a+b} \operatorname{Log}\left[-\operatorname{Sech}\left[\frac{x}{2}\right]^2\right] - \sqrt{a+b} \operatorname{Log}\left[a+b + \frac{\sqrt{a+b} \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a+b) \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] \right) \right) \right) \operatorname{Sech}\left[\frac{x}{2}\right]^2 \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2} \right) / \left(\sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4} \right)$$

Problem 213: Result more than twice size of optimal antiderivative.

$$\int \sqrt{a+b \operatorname{Tanh}[x]^2} dx$$

Optimal (type 3, 60 leaves, 6 steps):

$$-\sqrt{b} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^2}}\right] + \sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^2}}\right]$$

Result (type 3, 137 leaves):

$$\frac{1}{2} \left(-\sqrt{a+b} \operatorname{Log}[1 - \operatorname{Tanh}[x]] + \sqrt{a+b} \operatorname{Log}[1 + \operatorname{Tanh}[x]] - 2\sqrt{b} \operatorname{Log}[b \operatorname{Tanh}[x] + \sqrt{b} \sqrt{a+b \operatorname{Tanh}[x]^2}] - \sqrt{a+b} \operatorname{Log}[a - b \operatorname{Tanh}[x] + \sqrt{a+b} \sqrt{a+b \operatorname{Tanh}[x]^2}] + \sqrt{a+b} \operatorname{Log}[a + b \operatorname{Tanh}[x] + \sqrt{a+b} \sqrt{a+b \operatorname{Tanh}[x]^2}] \right)$$

Problem 214: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Coth}[x] \sqrt{a+b \operatorname{Tanh}[x]^2} dx$$

Optimal (type 3, 56 leaves, 7 steps):

$$-\sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a}}\right] + \sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right]$$

Result (type 3, 124 leaves):

$$-\left(\left(\operatorname{Cosh}[x] \left(\sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{2} \sqrt{a} \operatorname{Cosh}[x]}{\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}}\right] - \sqrt{a+b} \operatorname{Log}\left[\sqrt{2} \sqrt{a+b} \operatorname{Cosh}[x] + \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}\right] \right) \right) \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2} \right) / \left(\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \right)$$

Problem 215: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Coth}[x]^2 \sqrt{a+b \operatorname{Tanh}[x]^2} dx$$

Optimal (type 3, 48 leaves, 5 steps):

$$\sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b \operatorname{Tanh}[x]^2}}\right] - \operatorname{Coth}[x] \sqrt{a+b \operatorname{Tanh}[x]^2}$$

Result (type 4, 192 leaves):

$$\begin{aligned}
 & - \left(\left(\left((a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2 - \sqrt{2} (a + b) \sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right. \right. \right. \\
 & \quad \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}\right], 1\right] + \\
 & \quad \sqrt{2} a \sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \\
 & \quad \left. \left. \left. \operatorname{EllipticPi}\left[\frac{b}{a + b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}\right], 1\right] \operatorname{Tanh}[x] \right) \right) \right) / \\
 & \left. \left(\sqrt{2} \sqrt{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2} \right) \right)
 \end{aligned}$$

Problem 216: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Coth}[x]^3 \sqrt{a + b \operatorname{Tanh}[x]^2} dx$$

Optimal (type 3, 83 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{(2a + b) \operatorname{ArcTanh}\left[\frac{\sqrt{a + b \operatorname{Tanh}[x]^2}}{\sqrt{a}}\right]}{2\sqrt{a}} + \\
 & \sqrt{a + b} \operatorname{ArcTanh}\left[\frac{\sqrt{a + b \operatorname{Tanh}[x]^2}}{\sqrt{a + b}}\right] - \frac{1}{2} \operatorname{Coth}[x]^2 \sqrt{a + b \operatorname{Tanh}[x]^2}
 \end{aligned}$$

Result (type 3, 864 leaves):

$$\begin{aligned}
 & \sqrt{\frac{a - b + a \operatorname{Cosh}[2x] + b \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \left(-\frac{1}{2} - \frac{\operatorname{Csch}[x]^2}{2} \right) + \\
 & \frac{1}{2} \left((3a + b) (1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2x]}{(1 + \operatorname{Cosh}[x])^2}} \sqrt{\frac{a - b + (a + b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \operatorname{Log}\left[a + 2b + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] + \right. \\
 & \quad \left. \operatorname{Log}\left[a + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + 2b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) \\
 & \quad \left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) / \\
 & \quad \left(4\sqrt{a} \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) + \\
 & \quad \frac{1}{\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}} 3(a+b) \sqrt{1 + \operatorname{Cosh}[2x]} \sqrt{\frac{a-b+(a+b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \\
 & \quad \left(\left(4 \operatorname{Cosh}[x]^2 \sqrt{-2b+a(1+\operatorname{Cosh}[2x]) + b(1+\operatorname{Cosh}[2x])} \operatorname{Coth}[x] \right. \right. \\
 & \quad \left. \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{1+\operatorname{Cosh}[2x]}}{\sqrt{b(-1+\operatorname{Cosh}[2x]) + a(1+\operatorname{Cosh}[2x])}}\right]}{\sqrt{a}} + \frac{1}{\sqrt{a+b}} \operatorname{Log}\left[a \sqrt{1 + \operatorname{Cosh}[2x]} + b \right. \right. \\
 & \quad \left. \left. \sqrt{1 + \operatorname{Cosh}[2x]} + \sqrt{a+b} \sqrt{b(-1 + \operatorname{Cosh}[2x]) + a(1 + \operatorname{Cosh}[2x])} \right] \right) \right) \\
 & \quad \left. \operatorname{Sinh}[2x] \right) / \left(3(1 + \operatorname{Cosh}[2x])^2 \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \right) - \\
 & \quad \left((1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2x]}{(1 + \operatorname{Cosh}[x])^2}} \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[a + 2b + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[a + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + 2b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) \right)
 \end{aligned}$$

$$\left((-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right) \sqrt{\frac{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) / \left(4 \sqrt{a} \sqrt{1 + \operatorname{Cosh}[2 x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) \right)$$

Problem 217: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Coth}[x]^4 \sqrt{a + b \operatorname{Tanh}[x]^2} dx$$

Optimal (type 3, 78 leaves, 6 steps):

$$\sqrt{a + b} \operatorname{ArcTanh}\left[\frac{\sqrt{a + b} \operatorname{Tanh}[x]}{\sqrt{a + b \operatorname{Tanh}[x]^2}}\right] - \frac{(3 a + b) \operatorname{Coth}[x] \sqrt{a + b \operatorname{Tanh}[x]^2}}{3 a} - \frac{1}{3} \operatorname{Coth}[x]^3 \sqrt{a + b \operatorname{Tanh}[x]^2}$$

Result (type 4, 558 leaves):

$$\sqrt{\frac{a - b + a \operatorname{Cosh}[2 x] + b \operatorname{Cosh}[2 x]}{1 + \operatorname{Cosh}[2 x]}} \left(\frac{(-4 a \operatorname{Cosh}[x] - b \operatorname{Cosh}[x]) \operatorname{Csch}[x]}{3 a} - \frac{1}{3} \operatorname{Coth}[x] \operatorname{Csch}[x]^2 \right) + (a + b) \left(- \left(\left(b \sqrt{\frac{a - b + (a + b) \operatorname{Cosh}[2 x]}{1 + \operatorname{Cosh}[2 x]}} \sqrt{-\frac{a \operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \operatorname{Cosh}[2 x]) \operatorname{Csch}[x]^2}{b}} \right. \right. \right. \\ \left. \left. \sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2 x]) \operatorname{Csch}[x]^2}{b}} \operatorname{Csch}[2 x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2 x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \operatorname{Sinh}[x]^4 \right) / (a (a - b + (a + b) \operatorname{Cosh}[2 x])) \right) - \frac{1}{\sqrt{a - b + (a + b) \operatorname{Cosh}[2 x]}} 4 i b \sqrt{1 + \operatorname{Cosh}[2 x]} \sqrt{\frac{a - b + (a + b) \operatorname{Cosh}[2 x]}{1 + \operatorname{Cosh}[2 x]}}$$

$$\left(- \left(\left(\sqrt{-\frac{a \operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right. \right. \right.$$

$$\left. \left. \left. \sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \operatorname{Csch}[2x] \right. \right. \right.$$

$$\left. \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \operatorname{Sinh}[x]^4 \right) \right) /$$

$$\left(4 a \sqrt{1 + \operatorname{Cosh}[2x]} \sqrt{a-b + (a+b) \operatorname{Cosh}[2x]} \right) +$$

$$\left(\sqrt{-\frac{a \operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right.$$

$$\left. \left. \left. \operatorname{Csch}[2x] \operatorname{EllipticPi}\left[\frac{b}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \operatorname{Sinh}[x]^4 \right) \right) /$$

$$\left(2 (a+b) \sqrt{1 + \operatorname{Cosh}[2x]} \sqrt{a-b + (a+b) \operatorname{Cosh}[2x]} \right) \left. \right) \left. \right)$$

Problem 218: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Coth}[x]^5 \sqrt{a+b \operatorname{Tanh}[x]^2} dx$$

Optimal (type 3, 121 leaves, 9 steps):

$$-\frac{(8a^2 + 4ab - b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a}}\right]}{8a^{3/2}} + \sqrt{a+b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right] - \frac{(4a+b) \operatorname{Coth}[x]^2 \sqrt{a+b \operatorname{Tanh}[x]^2}}{8a} - \frac{1}{4} \operatorname{Coth}[x]^4 \sqrt{a+b \operatorname{Tanh}[x]^2}$$

Result (type 3, 911 leaves):

$$\sqrt{\frac{a-b+a \operatorname{Cosh}[2x]+b \operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \left(-\frac{6a+b}{8a} + \frac{(-8a-b) \operatorname{Csch}[x]^2}{8a} - \frac{\operatorname{Csch}[x]^4}{4} \right) + \frac{1}{4a} \left(\left((6a^2+2ab-b^2) (1+\operatorname{Cosh}[x]) \sqrt{\frac{1+\operatorname{Cosh}[2x]}{(1+\operatorname{Cosh}[x])^2}} \sqrt{\frac{a-b+(a+b) \operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \right. \right. \\ \left. \left. \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \operatorname{Log}\left[a+2b+a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) + \right. \right. \\ \left. \left. \operatorname{Log}\left[a+a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + 2b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) \right) \\ \left(-1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) / \\ \left(4\sqrt{a} \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \sqrt{\left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) + \\ \frac{1}{\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}} 3(2a^2+2ab) \sqrt{1+\operatorname{Cosh}[2x]} \sqrt{\frac{a-b+(a+b) \operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \\ \left(\left(4 \operatorname{Cosh}[x]^2 \sqrt{-2b+a(1+\operatorname{Cosh}[2x]) + b(1+\operatorname{Cosh}[2x])} \operatorname{Coth}[x] \right. \right. \\ \left. \left. \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{1+\operatorname{Cosh}[2x]}}{\sqrt{b(-1+\operatorname{Cosh}[2x]) + a(1+\operatorname{Cosh}[2x])}}\right]}{\sqrt{a}} + \frac{1}{\sqrt{a+b}} \operatorname{Log}\left[a \sqrt{1+\operatorname{Cosh}[2x]} + b \right. \right. \right. \\ \left. \left. \left. \sqrt{1+\operatorname{Cosh}[2x]} + \sqrt{a+b} \sqrt{b(-1+\operatorname{Cosh}[2x]) + a(1+\operatorname{Cosh}[2x])} \right] \right) \right) \right)$$

$$\begin{aligned}
 & \left. \text{Sinh}[2x] \right) / \left(3 (1 + \text{Cosh}[2x])^2 \sqrt{a - b + (a + b) \text{Cosh}[2x]} \right) - \\
 & \left((1 + \text{Cosh}[x]) \sqrt{\frac{1 + \text{Cosh}[2x]}{(1 + \text{Cosh}[x])^2}} \left(-\text{Log}\left[\text{Tanh}\left[\frac{x}{2}\right]^2\right] + \right. \right. \\
 & \quad \text{Log}\left[a + 2b + a \text{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \text{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right] + \right. \\
 & \quad \left. \text{Log}\left[a + a \text{Tanh}\left[\frac{x}{2}\right]^2 + 2b \text{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \text{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right] \right) \\
 & \quad \left. \left(-1 + \text{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \text{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) / \right. \\
 & \quad \left. \left(4 \sqrt{a} \sqrt{1 + \text{Cosh}[2x]} \sqrt{\left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \text{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) \right) \right)
 \end{aligned}$$

Problem 219: Result more than twice size of optimal antiderivative.

$$\int \text{Tanh}[x]^3 (a + b \text{Tanh}[x]^2)^{3/2} dx$$

Optimal (type 3, 82 leaves, 7 steps):

$$\begin{aligned}
 & (a + b)^{3/2} \text{ArcTanh}\left[\frac{\sqrt{a + b \text{Tanh}[x]^2}}{\sqrt{a + b}}\right] - \\
 & (a + b) \sqrt{a + b \text{Tanh}[x]^2} - \frac{1}{3} (a + b \text{Tanh}[x]^2)^{3/2} - \frac{(a + b \text{Tanh}[x]^2)^{5/2}}{5b}
 \end{aligned}$$

Result (type 3, 184 leaves):

$$\frac{1}{15\sqrt{2}} \sqrt{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Sech}[x]^2}$$

$$\left(-26a - \frac{3a^2}{b} - 23b - \left(15\sqrt{2}(a+b)^{3/2}\operatorname{Cosh}[x] \left(\operatorname{Log}\left[-\operatorname{Sech}\left[\frac{x}{2}\right]^2\right] - \operatorname{Log}\left[\right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \frac{\sqrt{a+b}\sqrt{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a+b)\operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right] \operatorname{Sech}\left[\frac{x}{2}\right]^2 \right) \right) \right) /$$

$$\left(\sqrt{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Sech}\left[\frac{x}{2}\right]^4} \right) + (6a+11b)\operatorname{Sech}[x]^2 - 3b\operatorname{Sech}[x]^4$$

Problem 220: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Tanh}[x]^2 (a+b\operatorname{Tanh}[x]^2)^{3/2} dx$$

Optimal (type 3, 123 leaves, 8 steps):

$$\frac{(3a^2 + 12ab + 8b^2)\operatorname{ArcTanh}\left[\frac{\sqrt{b}\operatorname{Tanh}[x]}{\sqrt{a+b\operatorname{Tanh}[x]^2}}\right]}{8\sqrt{b}} + (a+b)^{3/2}\operatorname{ArcTanh}\left[\frac{\sqrt{a+b}\operatorname{Tanh}[x]}{\sqrt{a+b\operatorname{Tanh}[x]^2}}\right] -$$

$$\frac{1}{8}(5a+4b)\operatorname{Tanh}[x]\sqrt{a+b\operatorname{Tanh}[x]^2} - \frac{1}{4}b\operatorname{Tanh}[x]^3\sqrt{a+b\operatorname{Tanh}[x]^2}$$

Result (type 4, 584 leaves):

$$\frac{1}{4} \left(\left(b(a^2 - 4ab - 4b^2) \sqrt{\frac{a-b+(a+b)\operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \sqrt{-\frac{a\operatorname{Coth}[x]^2}{b}} \right. \right.$$

$$\left. \left. \sqrt{-\frac{a(1+\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}} \sqrt{\frac{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}} \right) \right)$$

$$\begin{aligned}
 & \left. \text{Csch}[2x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\text{Cosh}[2x])\text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \text{Sinh}[x]^4 \right/ \\
 & \left. \left(a (a - b + (a + b) \text{Cosh}[2x]) \right) - \frac{1}{\sqrt{a - b + (a + b) \text{Cosh}[2x]}} \right. \\
 & 4 i b (4 a^2 + 8 a b + 4 b^2) \sqrt{1 + \text{Cosh}[2x]} \sqrt{\frac{a - b + (a + b) \text{Cosh}[2x]}{1 + \text{Cosh}[2x]}} \\
 & \left(- \left(\left(i \sqrt{-\frac{a \text{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\frac{(a - b + (a + b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \text{Csch}[2x] \right. \right. \right. \\
 & \left. \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\text{Cosh}[2x])\text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \text{Sinh}[x]^4 \right) \right/ \right. \\
 & \left. \left(4 a \sqrt{1 + \text{Cosh}[2x]} \sqrt{a - b + (a + b) \text{Cosh}[2x]} \right) + \right. \\
 & \left(i \sqrt{-\frac{a \text{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \sqrt{\frac{(a - b + (a + b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \right. \\
 & \left. \left. \left. \text{Csch}[2x] \text{EllipticPi}\left[\frac{b}{a + b}, \text{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\text{Cosh}[2x])\text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \text{Sinh}[x]^4 \right) \right/ \right.
 \end{aligned}$$

$$\left(2 (a + b) \sqrt{1 + \text{Cosh}[2x]} \sqrt{a - b + (a + b) \text{Cosh}[2x]} \right) \Bigg) +$$

$$\sqrt{\frac{a - b + a \text{Cosh}[2x] + b \text{Cosh}[2x]}{1 + \text{Cosh}[2x]}} \left(\frac{1}{8} \text{Sech}[x] (-5a \text{Sinh}[x] - 6b \text{Sinh}[x]) + \right.$$

$$\frac{1}{4} b$$

$$\left. \text{Sech}[x]^2 \text{Tanh}[x] \right)$$

Problem 221: Result more than twice size of optimal antiderivative.

$$\int \text{Tanh}[x] (a + b \text{Tanh}[x]^2)^{3/2} dx$$

Optimal (type 3, 63 leaves, 6 steps):

$$(a + b)^{3/2} \text{ArcTanh}\left[\frac{\sqrt{a + b \text{Tanh}[x]^2}}{\sqrt{a + b}}\right] - (a + b) \sqrt{a + b \text{Tanh}[x]^2} - \frac{1}{3} (a + b \text{Tanh}[x]^2)^{3/2}$$

Result (type 3, 164 leaves):

$$\frac{1}{\sqrt{2}} \sqrt{(a - b + (a + b) \text{Cosh}[2x]) \text{Sech}[x]^2}$$

$$\left(-\frac{4}{3} (a + b) - \left(\sqrt{2} (a + b)^{3/2} \text{Cosh}[x] \left(\text{Log}\left[-\text{Sech}\left[\frac{x}{2}\right]^2\right] - \text{Log}\left[\right. \right. \right. \right.$$

$$\left. \left. \left. a + b + \frac{\sqrt{a + b} \sqrt{(a - b + (a + b) \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a + b) \text{Tanh}\left[\frac{x}{2}\right]^2 \right) \text{Sech}\left[\frac{x}{2}\right]^2 \right) \right) /$$

$$\left(\sqrt{(a - b + (a + b) \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4} \right) + \frac{1}{3} b \text{Sech}[x]^2 \Bigg)$$

Problem 223: Result more than twice size of optimal antiderivative.

$$\int \text{Coth}[x] (a + b \text{Tanh}[x]^2)^{3/2} dx$$

Optimal (type 3, 71 leaves, 8 steps):

$$-a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a}}\right] + (a+b)^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right] - b \sqrt{a+b \operatorname{Tanh}[x]^2}$$

Result (type 3, 872 leaves):

$$\begin{aligned}
 & -b \sqrt{\frac{a-b+a \operatorname{Cosh}[2x]+b \operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} + \\
 & \frac{1}{2} \left(\left((3a^2-2ab-b^2)(1+\operatorname{Cosh}[x]) \sqrt{\frac{1+\operatorname{Cosh}[2x]}{(1+\operatorname{Cosh}[x])^2}} \sqrt{\frac{a-b+(a+b)\operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \right. \right. \\
 & \quad \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \operatorname{Log}\left[a+2b+a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a\left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right. \\
 & \quad \left. \left. \operatorname{Log}\left[a+a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + 2b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a\left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) \right) \\
 & \quad \left(-1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a\left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) / \\
 & \quad \left(4\sqrt{a} \sqrt{a-b+(a+b)\operatorname{Cosh}[2x]} \sqrt{\left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a\left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) + \\
 & \quad \frac{1}{\sqrt{a-b+(a+b)\operatorname{Cosh}[2x]}} 3(a^2+2ab+b^2) \sqrt{1+\operatorname{Cosh}[2x]} \sqrt{\frac{a-b+(a+b)\operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \\
 & \quad \left(\left(4 \operatorname{Cosh}[x]^2 \sqrt{-2b+a(1+\operatorname{Cosh}[2x]) + b(1+\operatorname{Cosh}[2x])} \operatorname{Coth}[x] \right. \right. \\
 & \quad \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a}\sqrt{1+\operatorname{Cosh}[2x]}}{\sqrt{b(-1+\operatorname{Cosh}[2x]) + a(1+\operatorname{Cosh}[2x])}}\right]}{\sqrt{a}} + \frac{1}{\sqrt{a+b}} \operatorname{Log}\left[a\sqrt{1+\operatorname{Cosh}[2x]} + b \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1+\operatorname{Cosh}[2x]} + \sqrt{a+b} \sqrt{b(-1+\operatorname{Cosh}[2x]) + a(1+\operatorname{Cosh}[2x])} \right] \right) \right)
 \end{aligned}$$

$$\left. \left. \left. \left. \left. \operatorname{Sinh}[2x] \right) \Big/ \left(3 (1 + \operatorname{Cosh}[2x])^2 \sqrt{a - b + (a + b) \operatorname{Cosh}[2x]} \right) - \right. \right. \right. \right. \right. \\ \left. \left((1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2x]}{(1 + \operatorname{Cosh}[x])^2}} \left(-\operatorname{Log} \left[\operatorname{Tanh} \left[\frac{x}{2} \right]^2 \right] + \right. \right. \right. \right. \right. \\ \left. \left. \operatorname{Log} \left[a + 2b + a \operatorname{Tanh} \left[\frac{x}{2} \right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh} \left[\frac{x}{2} \right]^2 + a (1 + \operatorname{Tanh} \left[\frac{x}{2} \right]^2)^2} \right] + \right. \right. \right. \\ \left. \left. \operatorname{Log} \left[a + a \operatorname{Tanh} \left[\frac{x}{2} \right]^2 + 2b \operatorname{Tanh} \left[\frac{x}{2} \right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh} \left[\frac{x}{2} \right]^2 + a (1 + \operatorname{Tanh} \left[\frac{x}{2} \right]^2)^2} \right] \right) \right. \\ \left. \left. \left. \left. \left. (-1 + \operatorname{Tanh} \left[\frac{x}{2} \right]^2) (1 + \operatorname{Tanh} \left[\frac{x}{2} \right]^2) \sqrt{\frac{4b \operatorname{Tanh} \left[\frac{x}{2} \right]^2 + a (1 + \operatorname{Tanh} \left[\frac{x}{2} \right]^2)^2}{(-1 + \operatorname{Tanh} \left[\frac{x}{2} \right]^2)^2}} \right) \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. \left(4 \sqrt{a} \sqrt{1 + \operatorname{Cosh}[2x]} \sqrt{(1 + \operatorname{Tanh} \left[\frac{x}{2} \right]^2)^2} \sqrt{4b \operatorname{Tanh} \left[\frac{x}{2} \right]^2 + a (1 + \operatorname{Tanh} \left[\frac{x}{2} \right]^2)^2} \right) \right) \right) \right) \right) \right) \right)$$

Problem 224: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Coth}[x]^2 (a + b \operatorname{Tanh}[x]^2)^{3/2} dx$$

Optimal (type 3, 77 leaves, 7 steps):

$$\begin{aligned} -b^{3/2} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \operatorname{Tanh}[x]}{\sqrt{a + b \operatorname{Tanh}[x]^2}} \right] + \\ (a + b)^{3/2} \operatorname{ArcTanh} \left[\frac{\sqrt{a + b} \operatorname{Tanh}[x]}{\sqrt{a + b \operatorname{Tanh}[x]^2}} \right] - a \operatorname{Coth}[x] \sqrt{a + b \operatorname{Tanh}[x]^2} \end{aligned}$$

Result (type 4, 197 leaves):

$$\begin{aligned}
 & - \left(\left(a \left((a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2 - \sqrt{2} (a+2b) \sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right. \right. \right. \\
 & \quad \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}} \right], 1 \right] + \\
 & \quad \sqrt{2} (a+b) \sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \\
 & \quad \left. \left. \left. \operatorname{EllipticPi} \left[\frac{b}{a+b}, \operatorname{ArcSin} \left[\frac{\sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}} \right], 1 \right] \operatorname{Tanh}[x] \right) \right) \right) / \\
 & \quad \left(\sqrt{2} \sqrt{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2} \right)
 \end{aligned}$$

Problem 229: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tanh}[x]^5}{\sqrt{a+b \operatorname{Tanh}[x]^2}} dx$$

Optimal (type 3, 70 leaves, 6 steps):

$$\frac{\operatorname{ArcTanh} \left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}} \right]}{\sqrt{a+b}} + \frac{(a-b) \sqrt{a+b \operatorname{Tanh}[x]^2}}{b^2} - \frac{(a+b \operatorname{Tanh}[x]^2)^{3/2}}{3b^2}$$

Result (type 3, 313 leaves):

$$\sqrt{\frac{a - b + a \operatorname{Cosh}[2x] + b \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \left(\frac{2(a - 2b)}{3b^2} + \frac{\operatorname{Sech}[x]^2}{3b} \right) +$$

$$\left((1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2x]}{(1 + \operatorname{Cosh}[x])^2}} \sqrt{\frac{a - b + (a + b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \left(\operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] - \right.$$

$$\left. \operatorname{Log}\left[a + b + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a + b} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right)$$

$$\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) /$$

$$\left(\sqrt{a + b} \sqrt{a - b + (a + b) \operatorname{Cosh}[2x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right)$$

Problem 230: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tanh}[x]^4}{\sqrt{a + b \operatorname{Tanh}[x]^2}} dx$$

Optimal (type 3, 88 leaves, 7 steps):

$$\frac{(a - 2b) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Tanh}[x]}{\sqrt{a + b \operatorname{Tanh}[x]^2}}\right]}{2b^{3/2}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a + b} \operatorname{Tanh}[x]}{\sqrt{a + b \operatorname{Tanh}[x]^2}}\right]}{\sqrt{a + b}} - \frac{\operatorname{Tanh}[x] \sqrt{a + b \operatorname{Tanh}[x]^2}}{2b}$$

Result (type 4, 542 leaves):

$$\frac{1}{b} \left(\left((a - b) b \sqrt{\frac{a - b + (a + b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \sqrt{-\frac{a \operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a(1 + \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right. \right.$$

$$\left. \sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \operatorname{Csch}[2x] \operatorname{EllipticF}\left[\right. \right.$$

$$\left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a - b + (a + b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}\right], 1 \right] \operatorname{Sinh}[x]^4 \right) / (a(a - b + (a + b) \operatorname{Cosh}[2x])) -$$

$$\begin{aligned}
 & \frac{1}{\sqrt{a-b+(a+b)\cosh[2x]}} 4 i b^2 \sqrt{1+\cosh[2x]} \sqrt{\frac{a-b+(a+b)\cosh[2x]}{1+\cosh[2x]}} \\
 & \left(- \left(\left(i \sqrt{-\frac{a\coth[x]^2}{b}} \sqrt{-\frac{a(1+\cosh[2x])\operatorname{csch}[x]^2}{b}} \right. \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(a-b+(a+b)\cosh[2x])\operatorname{csch}[x]^2}{b}} \operatorname{csch}[2x] \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\cosh[2x])\operatorname{csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \operatorname{Sinh}[x]^4 \right) \right) / \\
 & \quad \left. \left(4 a \sqrt{1+\cosh[2x]} \sqrt{a-b+(a+b)\cosh[2x]} \right) \right) + \\
 & \left(i \sqrt{-\frac{a\coth[x]^2}{b}} \sqrt{-\frac{a(1+\cosh[2x])\operatorname{csch}[x]^2}{b}} \sqrt{\frac{(a-b+(a+b)\cosh[2x])\operatorname{csch}[x]^2}{b}} \right. \\
 & \quad \left. \operatorname{csch}[2x] \operatorname{EllipticPi}\left[\frac{b}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\cosh[2x])\operatorname{csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \operatorname{Sinh}[x]^4 \right) / \\
 & \quad \left. \left(2(a+b)\sqrt{1+\cosh[2x]}\sqrt{a-b+(a+b)\cosh[2x]} \right) \right) - \\
 & \frac{\sqrt{\frac{a-b+a\cosh[2x]+b\cosh[2x]}{1+\cosh[2x]}} \operatorname{Tanh}[x]}{2b}
 \end{aligned}$$

Problem 231: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Tanh}[x]^3}{\sqrt{a + b \text{Tanh}[x]^2}} dx$$

Optimal (type 3, 47 leaves, 5 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{\sqrt{a+b}} - \frac{\sqrt{a+b \text{Tanh}[x]^2}}{b}$$

Result (type 3, 227 leaves):

$$- \left(\left(\text{Sech}\left[\frac{x}{2}\right]^2 \left(4 b \text{Cosh}[x] \text{Log}\left[-\text{Sech}\left[\frac{x}{2}\right]^2\right] - \right. \right. \right. \\ \left. \left. 4 b \text{Cosh}[x] \text{Log}\left[a + b + \frac{\sqrt{a+b} \sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}}}\right] + (a+b) \text{Tanh}\left[\frac{x}{2}\right]^2 \right) + \right. \\ \left. \sqrt{2} \sqrt{a+b} \sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4} + \sqrt{2} \sqrt{a+b} \text{Cosh}[x] \right. \\ \left. \left. \left. \sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4} \right) \sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}[x]^2} \right) / \right. \\ \left. \left. \left(4 b \sqrt{a+b} \sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}\left[\frac{x}{2}\right]^4} \right) \right) \right)$$

Problem 232: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Tanh}[x]^2}{\sqrt{a + b \text{Tanh}[x]^2}} dx$$

Optimal (type 3, 60 leaves, 6 steps):

$$- \frac{\text{ArcTanh}\left[\frac{\sqrt{b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{\sqrt{b}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{\sqrt{a+b}}$$

Result (type 4, 101 leaves):

$$\left(\left(a \operatorname{Coth}[x] \operatorname{EllipticPi}\left[\frac{b}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}}{b}}{\sqrt{2}}\right], 1\right] \right. \right.$$

$$\left. \left. \sqrt{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Sech}[x]^2} \right) / \left(b(a+b) \sqrt{\frac{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}} \right) \right)$$

Problem 233: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tanh}[x]}{\sqrt{a+b\operatorname{Tanh}[x]^2}} dx$$

Optimal (type 3, 29 leaves, 4 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b\operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{\sqrt{a+b}}$$

Result (type 3, 136 leaves):

$$\left(\left(\operatorname{Cosh}[x] \left(\operatorname{Log}\left[-\operatorname{Sech}\left[\frac{x}{2}\right]^2\right] - \right. \right. \right.$$

$$\left. \left. \operatorname{Log}\left[a+b + \frac{\sqrt{a+b}\sqrt{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} + (a+b)\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] \right) \operatorname{Sech}\left[\frac{x}{2}\right]^2 \right.$$

$$\left. \left. \sqrt{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Sech}[x]^2} \right) / \left(\sqrt{a+b}\sqrt{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Sech}\left[\frac{x}{2}\right]^4} \right) \right)$$

Problem 234: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{a+b\operatorname{Tanh}[x]^2}} dx$$

Optimal (type 3, 31 leaves, 3 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{\sqrt{a+b}}$$

Result (type 3, 83 leaves):

$$\frac{1}{2\sqrt{a+b}} \left(-\text{Log}[1 - \text{Tanh}[x]] + \text{Log}[1 + \text{Tanh}[x]] - \text{Log}\left[a - b \text{Tanh}[x] + \sqrt{a+b} \sqrt{a+b \text{Tanh}[x]^2} \right] + \text{Log}\left[a + b \text{Tanh}[x] + \sqrt{a+b} \sqrt{a+b \text{Tanh}[x]^2} \right] \right)$$

Problem 235: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Coth}[x]}{\sqrt{a+b \text{Tanh}[x]^2}} dx$$

Optimal (type 3, 56 leaves, 7 steps):

$$-\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a}}\right]}{\sqrt{a}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{\sqrt{a+b}}$$

Result (type 3, 161 leaves):

$$\left(\sqrt{\text{Cosh}[x]^2} \left(-\sqrt{a+b} \text{ArcTanh}\left[\frac{\sqrt{a} \sqrt{1 + \text{Cosh}[2x]}}{\sqrt{a-b + (a+b) \text{Cosh}[2x]}} \right] + \sqrt{a} \text{Log}\left[a \sqrt{1 + \text{Cosh}[2x]} + b \sqrt{1 + \text{Cosh}[2x]} + \sqrt{a+b} \sqrt{a-b + (a+b) \text{Cosh}[2x]} \right] \right) \right) / \left(\sqrt{a-b + (a+b) \text{Cosh}[2x]} \text{Sech}[x]^2 \right)$$

Problem 236: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Coth}[x]^2}{\sqrt{a+b \text{Tanh}[x]^2}} dx$$

Optimal (type 3, 51 leaves, 5 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{\sqrt{a+b}} - \frac{\text{Coth}[x] \sqrt{a+b \text{Tanh}[x]^2}}{a}$$

Result (type 4, 206 leaves):

$$\begin{aligned}
 & - \left(\left(\left((a+b) (a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2 - \right. \right. \right. \\
 & \quad \sqrt{2} a (a+b) \sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \operatorname{EllipticF}\left[\right. \\
 & \quad \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}\right], 1 \right] + \sqrt{2} a^2 \sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \\
 & \quad \left. \left. \left. \operatorname{EllipticPi}\left[\frac{b}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}\right], 1 \right] \operatorname{Tanh}[x] \right) \right) \right) / \\
 & \left. \left(\sqrt{2} a (a+b) \sqrt{(a-b + (a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2} \right) \right)
 \end{aligned}$$

Problem 237: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Coth}[x]^3}{\sqrt{a+b \operatorname{Tanh}[x]^2}} dx$$

Optimal (type 3, 88 leaves, 8 steps):

$$-\frac{(2a-b) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a}}\right]}{2a^{3/2}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{\sqrt{a+b}} - \frac{\operatorname{Coth}[x]^2 \sqrt{a+b \operatorname{Tanh}[x]^2}}{2a}$$

Result (type 3, 874 leaves):

$$\begin{aligned}
 & \sqrt{\frac{a-b+a \operatorname{Cosh}[2x]+b \operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \left(-\frac{1}{2a} - \frac{\operatorname{Csch}[x]^2}{2a} \right) + \\
 & \frac{1}{2a} \left(\left((3a-2b) (1+\operatorname{Cosh}[x]) \sqrt{\frac{1+\operatorname{Cosh}[2x]}{(1+\operatorname{Cosh}[x])^2}} \sqrt{\frac{a-b+(a+b) \operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \right. \right. \\
 & \quad \left. \left. \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \operatorname{Log}\left[a+2b+a \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2+a \left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\text{Log} \left[a + a \text{Tanh} \left[\frac{x}{2} \right]^2 + 2 b \text{Tanh} \left[\frac{x}{2} \right]^2 + \sqrt{a} \sqrt{4 b \text{Tanh} \left[\frac{x}{2} \right]^2 + a \left(1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right)^2} \right] \right) \\
 & \left(-1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right) \left(1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right) \sqrt{\frac{4 b \text{Tanh} \left[\frac{x}{2} \right]^2 + a \left(1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right)^2}{\left(-1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right)^2}} \right) / \\
 & \left(4 \sqrt{a} \sqrt{a - b + (a + b) \text{Cosh} [2 x]} \sqrt{\left(1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right)^2} \sqrt{4 b \text{Tanh} \left[\frac{x}{2} \right]^2 + a \left(1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right)^2} \right) + \\
 & \frac{1}{\sqrt{a - b + (a + b) \text{Cosh} [2 x]}} 3 a \sqrt{1 + \text{Cosh} [2 x]} \sqrt{\frac{a - b + (a + b) \text{Cosh} [2 x]}{1 + \text{Cosh} [2 x]}} \\
 & \left(\left(4 \text{Cosh} [x]^2 \sqrt{-2 b + a (1 + \text{Cosh} [2 x]) + b (1 + \text{Cosh} [2 x])} \text{Coth} [x] \right. \right. \\
 & \left. \left(- \frac{\text{ArcTanh} \left[\frac{\sqrt{a} \sqrt{1 + \text{Cosh} [2 x]}}{\sqrt{b (-1 + \text{Cosh} [2 x]) + a (1 + \text{Cosh} [2 x])}} \right]}{\sqrt{a}} + \frac{1}{\sqrt{a + b}} \text{Log} [a \sqrt{1 + \text{Cosh} [2 x]} + b \right. \right. \\
 & \left. \left. \sqrt{1 + \text{Cosh} [2 x]} + \sqrt{a + b} \sqrt{b (-1 + \text{Cosh} [2 x]) + a (1 + \text{Cosh} [2 x])} \right] \right) \\
 & \left. \text{Sinh} [2 x] \right) / \left(3 (1 + \text{Cosh} [2 x])^2 \sqrt{a - b + (a + b) \text{Cosh} [2 x]} \right) - \\
 & \left((1 + \text{Cosh} [x]) \sqrt{\frac{1 + \text{Cosh} [2 x]}{(1 + \text{Cosh} [x])^2}} \left(-\text{Log} \left[\text{Tanh} \left[\frac{x}{2} \right]^2 \right] + \right. \right. \\
 & \left. \left. \text{Log} [a + 2 b + a \text{Tanh} \left[\frac{x}{2} \right]^2 + \sqrt{a} \sqrt{4 b \text{Tanh} \left[\frac{x}{2} \right]^2 + a \left(1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right)^2} \right] + \right. \\
 & \left. \left. \text{Log} [a + a \text{Tanh} \left[\frac{x}{2} \right]^2 + 2 b \text{Tanh} \left[\frac{x}{2} \right]^2 + \sqrt{a} \sqrt{4 b \text{Tanh} \left[\frac{x}{2} \right]^2 + a \left(1 + \text{Tanh} \left[\frac{x}{2} \right]^2 \right)^2} \right] \right)
 \end{aligned}$$

$$\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2}} \right) /$$

$$\left(4 \sqrt{a} \sqrt{1 + \operatorname{Cosh}[2 x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2} \sqrt{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2} \right) \right)$$

Problem 238: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tanh}[x]^5}{(a + b \operatorname{Tanh}[x]^2)^{3/2}} dx$$

Optimal (type 3, 72 leaves, 6 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} - \frac{a^2}{b^2 (a+b) \sqrt{a+b \operatorname{Tanh}[x]^2}} - \frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{b^2}$$

Result (type 3, 200 leaves):

$$\frac{1}{\sqrt{2}} \left(\frac{-2 a^2 + b^2 - (2 a^2 + 2 a b + b^2) \operatorname{Cosh}[2 x]}{b^2 (a+b) (a-b + (a+b) \operatorname{Cosh}[2 x])} - \right.$$

$$\left. \left(\sqrt{2} \operatorname{Cosh}[x] \left(\operatorname{Log}\left[-\operatorname{Sech}\left[\frac{x}{2}\right]^2\right] - \operatorname{Log}[a+b] + \frac{\sqrt{a+b} \sqrt{(a-b + (a+b) \operatorname{Cosh}[2 x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}} \right) \right) \right) \right)$$

$$\left. \left((a+b) \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \operatorname{Sech}\left[\frac{x}{2}\right]^2 \right) /$$

$$\left((a+b)^{3/2} \sqrt{(a-b + (a+b) \operatorname{Cosh}[2 x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4} \right) \sqrt{(a-b + (a+b) \operatorname{Cosh}[2 x]) \operatorname{Sech}[x]^2}$$

Problem 239: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Tanh}[x]^4}{(a + b \text{Tanh}[x]^2)^{3/2}} dx$$

Optimal (type 3, 84 leaves, 7 steps):

$$-\frac{\text{ArcTanh}\left[\frac{\sqrt{b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{b^{3/2}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a-b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{(a+b)^{3/2}} + \frac{a \text{Tanh}[x]}{b(a+b)\sqrt{a+b \text{Tanh}[x]^2}}$$

Result (type 4, 188 leaves):

$$-\left(\left(a \left(-2a - 2b + \sqrt{2} (a+b) \sqrt{\frac{(a-b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}}}{\sqrt{2}}}, 1 \right] + \sqrt{2} b \sqrt{\frac{(a-b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \right. \right. \right. \\ \left. \left. \left. \text{EllipticPi}\left[\frac{b}{a+b}, \text{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}}}{\sqrt{2}}}, 1 \right] \right] \text{Tanh}[x] \right) \right) / \right. \\ \left. \left(\sqrt{2} b (a+b)^2 \sqrt{(a-b+(a+b) \text{Cosh}[2x]) \text{Sech}[x]^2} \right) \right)$$

Problem 240: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Tanh}[x]^3}{(a + b \text{Tanh}[x]^2)^{3/2}} dx$$

Optimal (type 3, 52 leaves, 5 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} + \frac{a}{b(a+b)\sqrt{a+b \text{Tanh}[x]^2}}$$

Result (type 3, 178 leaves):

$$\frac{1}{\sqrt{2}} \left(\frac{2 a \operatorname{Cosh}[x]^2}{b (a+b) (a-b+(a+b) \operatorname{Cosh}[2 x])} - \left(\sqrt{2} \operatorname{Cosh}[x] \left(\operatorname{Log}\left[-\operatorname{Sech}\left[\frac{x}{2}\right]^2\right] - \operatorname{Log}\left[a+b+\frac{\sqrt{a+b} \sqrt{(a-b+(a+b) \operatorname{Cosh}[2 x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}}}\right] + (a+b) \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \operatorname{Sech}\left[\frac{x}{2}\right]^2 \right) / \left((a+b)^{3/2} \sqrt{(a-b+(a+b) \operatorname{Cosh}[2 x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4} \right) \right) \sqrt{(a-b+(a+b) \operatorname{Cosh}[2 x]) \operatorname{Sech}[x]^2}$$

Problem 241: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tanh}[x]^2}{(a+b \operatorname{Tanh}[x]^2)^{3/2}} dx$$

Optimal (type 3, 53 leaves, 4 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^2}}\right]}{(a+b)^{3/2}} - \frac{\operatorname{Tanh}[x]}{(a+b) \sqrt{a+b \operatorname{Tanh}[x]^2}}$$

Result (type 4, 182 leaves):

$$\left(\left(\sqrt{2} (a+b) \sqrt{\frac{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right. \right. \\ \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] - \right. \\ \left. 2 \left(a+b + \frac{1}{\sqrt{2}} a \sqrt{\frac{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}} \right. \right. \\ \left. \left. \operatorname{EllipticPi}\left[\frac{b}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \right) \right) \operatorname{Tanh}[x] \Big/ \\ \left(\sqrt{2} (a+b)^2 \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2} \right)$$

Problem 242: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tanh}[x]}{(a+b \operatorname{Tanh}[x]^2)^{3/2}} dx$$

Optimal (type 3, 49 leaves, 5 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} - \frac{1}{(a+b) \sqrt{a+b \operatorname{Tanh}[x]^2}}$$

Result (type 3, 174 leaves):

$$\frac{1}{\sqrt{2}} \left(-\frac{2 \operatorname{Cosh}[x]^2}{(a+b)(a-b+(a+b)\operatorname{Cosh}[2x])} - \left(\sqrt{2} \operatorname{Cosh}[x] \left(\operatorname{Log}\left[-\operatorname{Sech}\left[\frac{x}{2}\right]^2\right] - \operatorname{Log}\left[a+b + \frac{\sqrt{a+b} \sqrt{(a-b+(a+b)\operatorname{Cosh}[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4}}{\sqrt{2}}}\right] + (a+b) \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \operatorname{Sech}\left[\frac{x}{2}\right]^2 \right) \right) \left((a+b)^{3/2} \sqrt{(a-b+(a+b)\operatorname{Cosh}[2x]) \operatorname{Sech}\left[\frac{x}{2}\right]^4} \right) \sqrt{(a-b+(a+b)\operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2}$$

Problem 244: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Coth}[x]}{(a+b \operatorname{Tanh}[x]^2)^{3/2}} dx$$

Optimal (type 3, 78 leaves, 8 steps):

$$-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a}}\right]}{a^{3/2}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{3/2}} + \frac{b}{a(a+b)\sqrt{a+b \operatorname{Tanh}[x]^2}}$$

Result (type 3, 903 leaves):

$$\sqrt{\frac{a-b+a \operatorname{Cosh}[2x]+b \operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \left(\frac{b}{a(a+b)^2} + \frac{2b^2}{a(a+b)^2(a-b+a \operatorname{Cosh}[2x]+b \operatorname{Cosh}[2x])} \right) + \frac{1}{2a(a+b)} \left(\left((3a+4b)(1+\operatorname{Cosh}[x]) \sqrt{\frac{1+\operatorname{Cosh}[2x]}{(1+\operatorname{Cosh}[x])^2}} \sqrt{\frac{a-b+(a+b)\operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \right. \right. \\ \left. \left. \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \operatorname{Log}\left[a+2b+a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a\left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) + \operatorname{Log}\left[a+a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + 2b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a\left(1+\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right)$$

$$\begin{aligned}
 & \left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2}} \right) / \\
 & \left(4 \sqrt{a} \sqrt{a - b + (a + b) \operatorname{Cosh}[2 x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2} \sqrt{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2} \right) + \\
 & \frac{1}{\sqrt{a - b + (a + b) \operatorname{Cosh}[2 x]}} 3 a \sqrt{1 + \operatorname{Cosh}[2 x]} \sqrt{\frac{a - b + (a + b) \operatorname{Cosh}[2 x]}{1 + \operatorname{Cosh}[2 x]}} \\
 & \left(\left(4 \operatorname{Cosh}[x]^2 \sqrt{-2 b + a (1 + \operatorname{Cosh}[2 x]) + b (1 + \operatorname{Cosh}[2 x])} \operatorname{Coth}[x] \right. \right. \\
 & \left. \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{1 + \operatorname{Cosh}[2 x]}}{\sqrt{b (-1 + \operatorname{Cosh}[2 x]) + a (1 + \operatorname{Cosh}[2 x])}}\right]}{\sqrt{a}} + \frac{1}{\sqrt{a + b}} \operatorname{Log}\left[a \sqrt{1 + \operatorname{Cosh}[2 x]} + b \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \operatorname{Cosh}[2 x]} + \sqrt{a + b} \sqrt{b (-1 + \operatorname{Cosh}[2 x]) + a (1 + \operatorname{Cosh}[2 x])} \right] \right) \right) \\
 & \left. \operatorname{Sinh}[2 x] \right) / \left(3 (1 + \operatorname{Cosh}[2 x])^2 \sqrt{a - b + (a + b) \operatorname{Cosh}[2 x]} \right) - \\
 & \left((1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2 x]}{(1 + \operatorname{Cosh}[x])^2}} \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \right. \right. \\
 & \left. \left. \operatorname{Log}\left[a + 2 b + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2}\right] + \right. \right. \\
 & \left. \left. \operatorname{Log}\left[a + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + 2 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2}\right] \right) \right) \\
 & \left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4 b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right)^2}} \right) /
 \end{aligned}$$

$$\left(4 \sqrt{a} \sqrt{1 + \text{Cosh}[2x]} \sqrt{\left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \text{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right)$$

Problem 245: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Coth}[x]^2}{(a + b \text{Tanh}[x]^2)^{3/2}} dx$$

Optimal (type 3, 85 leaves, 6 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{(a+b)^{3/2}} + \frac{b \text{Coth}[x]}{a(a+b) \sqrt{a+b \text{Tanh}[x]^2}} - \frac{(a+2b) \text{Coth}[x] \sqrt{a+b \text{Tanh}[x]^2}}{a^2(a+b)}$$

Result (type 4, 230 leaves):

$$\left(\left((a+b) (a^2 - 2b^2 + (a^2 + 2ab + 2b^2) \text{Cosh}[2x]) \text{Csch}[x]^2 - \sqrt{2} a^2 (a+b) \sqrt{\frac{(a-b + (a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{\frac{(a-b + (a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] + \sqrt{2} a^3 \sqrt{\frac{(a-b + (a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \text{EllipticPi}\left[\frac{b}{a+b}, \text{ArcSin}\left[\frac{\sqrt{\frac{(a-b + (a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \text{Sech}[x]^2 \text{Sinh}[2x] \right) / \left(2 \sqrt{2} a^2 (a+b)^2 \sqrt{(a-b + (a+b) \text{Cosh}[2x]) \text{Sech}[x]^2} \right)$$

Problem 246: Result unnecessarily involves higher level functions.

$$\int \frac{\text{Tanh}[x]^6}{(a + b \text{Tanh}[x]^2)^{5/2}} dx$$

Optimal (type 3, 118 leaves, 8 steps):

$$-\frac{\text{ArcTanh}\left[\frac{\sqrt{b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{b^{5/2}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a-b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{(a+b)^{5/2}} + \frac{a \text{Tanh}[x]^3}{3 b (a+b) (a+b \text{Tanh}[x]^2)^{3/2}} + \frac{a (a+2 b) \text{Tanh}[x]}{b^2 (a+b)^2 \sqrt{a+b \text{Tanh}[x]^2}}$$

Result (type 4, 231 leaves):

$$\frac{1}{3 \sqrt{2} b^2 (a+b)^3} \sqrt{(a-b+(a+b) \text{Cosh}[2 x]) \text{Sech}[x]^2} \left(- \left(\left(\left(3 \sqrt{2} a \text{Coth}[x] \left((a^2 + 3 a b + 2 b^2) \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{(a-b+(a+b) \text{Cosh}[2 x]) \text{Csch}[x]^2}}{b}\right], 1\right] + b^2 \text{EllipticPi}\left[\frac{b}{a+b}, \text{ArcSin}\left[\frac{\sqrt{(a-b+(a+b) \text{Cosh}[2 x]) \text{Csch}[x]^2}}{b}\right], 1\right] \right) \right) \right) / \left(b \sqrt{\frac{(a-b+(a+b) \text{Cosh}[2 x]) \text{Csch}[x]^2}{b}} \right) + (a (a+b) (3 a^2 + 2 a b - 7 b^2 + (3 a^2 + 10 a b + 7 b^2) \text{Cosh}[2 x]) \text{Sinh}[2 x]) / (a-b+(a+b) \text{Cosh}[2 x])^2 \right)$$

Problem 247: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Tanh}[x]^5}{(a + b \text{Tanh}[x]^2)^{5/2}} dx$$

Optimal (type 3, 84 leaves, 6 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \tanh[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{5/2}} - \frac{a^2}{3b^2(a+b)(a+b \tanh[x]^2)^{3/2}} + \frac{a(a+2b)}{b^2(a+b)^2 \sqrt{a+b \tanh[x]^2}}$$

Result (type 3, 376 leaves):

$$\begin{aligned} & \sqrt{\frac{a-b+a \cosh[2x]+b \cosh[2x]}{1+\cosh[2x]}} \left(\frac{2a(a+3b)}{3b^2(a+b)^3} - \right. \\ & \left. \frac{4a^2}{3(a+b)^3(a-b+a \cosh[2x]+b \cosh[2x])^2} + \frac{2a(a+6b)}{3b(a+b)^3(a-b+a \cosh[2x]+b \cosh[2x])} \right) + \\ & \left((1+\cosh[x]) \sqrt{\frac{1+\cosh[2x]}{(1+\cosh[x])^2}} \sqrt{\frac{a-b+(a+b) \cosh[2x]}{1+\cosh[2x]}} \left(\text{Log}\left[-1+\tanh\left[\frac{x}{2}\right]^2\right] - \right. \right. \\ & \left. \left. \text{Log}\left[a+b+a \tanh\left[\frac{x}{2}\right]^2+b \tanh\left[\frac{x}{2}\right]^2+\sqrt{a+b} \sqrt{4b \tanh\left[\frac{x}{2}\right]^2+a\left(1+\tanh\left[\frac{x}{2}\right]^2\right)^2}\right] \right) \right. \\ & \left. (-1+\tanh\left[\frac{x}{2}\right]^2\right) \left(1+\tanh\left[\frac{x}{2}\right]^2\right) \sqrt{\frac{4b \tanh\left[\frac{x}{2}\right]^2+a\left(1+\tanh\left[\frac{x}{2}\right]^2\right)^2}{(-1+\tanh\left[\frac{x}{2}\right]^2)^2}} \right) \Big/ \\ & \left((a+b)^{5/2} \sqrt{a-b+(a+b) \cosh[2x]} \sqrt{\left(1+\tanh\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \tanh\left[\frac{x}{2}\right]^2+a\left(1+\tanh\left[\frac{x}{2}\right]^2\right)^2} \right) \end{aligned}$$

Problem 248: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\tanh[x]^4}{(a+b \tanh[x]^2)^{5/2}} dx$$

Optimal (type 3, 90 leaves, 6 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \tanh[x]}}{\sqrt{a+b \tanh[x]^2}}\right]}{(a+b)^{5/2}} + \frac{a \tanh[x]}{3b(a+b)(a+b \tanh[x]^2)^{3/2}} - \frac{(a+4b) \tanh[x]}{3b(a+b)^2 \sqrt{a+b \tanh[x]^2}}$$

Result (type 4, 595 leaves):

$$\frac{1}{(a+b)^2} \left(- \left(\left(b \sqrt{\frac{a-b+(a+b) \cosh[2x]}{1+\cosh[2x]}} \sqrt{-\frac{a \coth[x]^2}{b}} \sqrt{-\frac{a(1+\cosh[2x]) \text{Csch}[x]^2}{b}} \right) \right) \right)$$

$$\begin{aligned}
 & \sqrt{\frac{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}} \operatorname{Csch}[2x] \operatorname{EllipticF}\left[\right. \\
 & \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}\right], 1\right] \operatorname{Sinh}[x]^4 \left. \right] / (a(a-b+(a+b)\operatorname{Cosh}[2x])) - \\
 & \frac{1}{\sqrt{a-b+(a+b)\operatorname{Cosh}[2x]}} 4 i b \sqrt{1+\operatorname{Cosh}[2x]} \sqrt{\frac{a-b+(a+b)\operatorname{Cosh}[2x]}{1+\operatorname{Cosh}[2x]}} \\
 & \left(- \left(\left(i \sqrt{-\frac{a\operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a(1+\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}} \right. \right. \right. \\
 & \left. \left. \sqrt{\frac{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}} \operatorname{Csch}[2x] \right. \right. \\
 & \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}\right], 1\right] \operatorname{Sinh}[x]^4 \right) / \right. \\
 & \left. \left(4 a \sqrt{1+\operatorname{Cosh}[2x]} \sqrt{a-b+(a+b)\operatorname{Cosh}[2x]} \right) \right) + \\
 & \left(i \sqrt{-\frac{a\operatorname{Coth}[x]^2}{b}} \sqrt{-\frac{a(1+\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}} \sqrt{\frac{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}} \right. \\
 & \left. \operatorname{Csch}[2x] \operatorname{EllipticPi}\left[\frac{b}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{(a-b+(a+b)\operatorname{Cosh}[2x])\operatorname{Csch}[x]^2}{b}}}{\sqrt{2}}\right], 1\right] \operatorname{Sinh}[x]^4 \right) /
 \end{aligned}$$

$$\left. \left(2 (a+b) \sqrt{1 + \text{Cosh}[2x]} \sqrt{a-b + (a+b) \text{Cosh}[2x]} \right) \right) +$$

$$\sqrt{\frac{a-b + a \text{Cosh}[2x] + b \text{Cosh}[2x]}{1 + \text{Cosh}[2x]}} \left(\frac{2a \text{Sinh}[2x]}{3(a+b)^2 (a-b + a \text{Cosh}[2x] + b \text{Cosh}[2x])^2} - \right.$$

$$\left. \frac{4 \text{Sinh}[2x]}{3(a+b)^2 (a-b + a \text{Cosh}[2x] + b \text{Cosh}[2x])} \right)$$

Problem 249: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Tanh}[x]^3}{(a+b \text{Tanh}[x]^2)^{5/2}} dx$$

Optimal (type 3, 74 leaves, 6 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{5/2}} + \frac{a}{3b(a+b)(a+b \text{Tanh}[x]^2)^{3/2}} - \frac{1}{(a+b)^2 \sqrt{a+b \text{Tanh}[x]^2}}$$

Result (type 3, 372 leaves):

$$\sqrt{\frac{a-b + a \text{Cosh}[2x] + b \text{Cosh}[2x]}{1 + \text{Cosh}[2x]}} \left(\frac{a-3b}{3b(a+b)^3} + \right.$$

$$\left. \frac{4ab}{3(a+b)^3 (a-b + a \text{Cosh}[2x] + b \text{Cosh}[2x])^2} + \frac{2(2a-3b)}{3(a+b)^3 (a-b + a \text{Cosh}[2x] + b \text{Cosh}[2x])} \right) +$$

$$\left((1 + \text{Cosh}[x]) \sqrt{\frac{1 + \text{Cosh}[2x]}{(1 + \text{Cosh}[x])^2}} \sqrt{\frac{a-b + (a+b) \text{Cosh}[2x]}{1 + \text{Cosh}[2x]}} \left(\text{Log}\left[-1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right] - \right.$$

$$\left. \text{Log}\left[a+b + a \text{Tanh}\left[\frac{x}{2}\right]^2 + b \text{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a+b} \sqrt{4b \text{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right)$$

$$\left(-1 + \text{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \text{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) /$$

$$\left((a+b)^{5/2} \sqrt{a-b + (a+b) \text{Cosh}[2x]} \sqrt{\left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \text{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \text{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right)$$

Problem 250: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{\text{Tanh}[x]^2}{(a + b \text{Tanh}[x]^2)^{5/2}} dx$$

Optimal (type 3, 88 leaves, 6 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+b} \text{Tanh}[x]}{\sqrt{a+b \text{Tanh}[x]^2}}\right]}{(a+b)^{5/2}} - \frac{\text{Tanh}[x]}{3(a+b)(a+b \text{Tanh}[x]^2)^{3/2}} - \frac{(2a-b) \text{Tanh}[x]}{3a(a+b)^2 \sqrt{a+b \text{Tanh}[x]^2}}$$

Result (type 4, 608 leaves):

$$\frac{1}{(a+b)^2} \left(- \left(\left(\left(b \sqrt{\frac{a-b+(a+b) \text{Cosh}[2x]}{1+\text{Cosh}[2x]}} \sqrt{-\frac{a \text{Coth}[x]^2}{b}} \sqrt{-\frac{a(1+\text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \right. \right. \right. \right. \\ \left. \left. \left. \sqrt{\frac{(a-b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \text{Csch}[2x] \text{EllipticF}\left[\right. \right. \right. \right. \\ \left. \left. \left. \text{ArcSin}\left[\sqrt{\frac{(a-b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}}\right], 1\right] \text{Sinh}[x]^4 \right) \right) \right) / (a(a-b+(a+b) \text{Cosh}[2x])) - \\ \frac{1}{\sqrt{a-b+(a+b) \text{Cosh}[2x]}} 4 i b \sqrt{1+\text{Cosh}[2x]} \sqrt{\frac{a-b+(a+b) \text{Cosh}[2x]}{1+\text{Cosh}[2x]}} \\ \left(- \left(\left(\left(i \sqrt{-\frac{a \text{Coth}[x]^2}{b}} \sqrt{-\frac{a(1+\text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \right. \right. \right. \right. \\ \left. \left. \left. \sqrt{\frac{(a-b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}} \text{Csch}[2x] \right. \right. \right. \\ \left. \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{(a-b+(a+b) \text{Cosh}[2x]) \text{Csch}[x]^2}{b}}\right], 1\right] \text{Sinh}[x]^4 \right) \right) \right) /$$

$$\left(4 a \sqrt{1 + \text{Cosh}[2 x]} \sqrt{a - b + (a + b) \text{Cosh}[2 x]} \right) +$$

$$\left(i \sqrt{-\frac{a \text{Coth}[x]^2}{b}} \sqrt{-\frac{a (1 + \text{Cosh}[2 x]) \text{Csch}[x]^2}{b}} \sqrt{\frac{(a - b + (a + b) \text{Cosh}[2 x]) \text{Csch}[x]^2}{b}} \right.$$

$$\left. \text{Csch}[2 x] \text{EllipticPi}\left[\frac{b}{a + b}, \text{ArcSin}\left[\frac{\sqrt{\frac{(a - b + (a + b) \text{Cosh}[2 x]) \text{Csch}[x]^2}{b}}}{\sqrt{2}}}\right], 1\right] \text{Sinh}[x]^4 \right) /$$

$$\left(2 (a + b) \sqrt{1 + \text{Cosh}[2 x]} \sqrt{a - b + (a + b) \text{Cosh}[2 x]} \right) \left. \right) +$$

$$\sqrt{\frac{a - b + a \text{Cosh}[2 x] + b \text{Cosh}[2 x]}{1 + \text{Cosh}[2 x]}} \left(-\frac{2 b \text{Sinh}[2 x]}{3 (a + b)^2 (a - b + a \text{Cosh}[2 x] + b \text{Cosh}[2 x])^2} + \right.$$

$$\left. \frac{-3 a \text{Sinh}[2 x] + b \text{Sinh}[2 x]}{3 a (a + b)^2 (a - b + a \text{Cosh}[2 x] + b \text{Cosh}[2 x])} \right)$$

Problem 251: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Tanh}[x]}{(a + b \text{Tanh}[x]^2)^{5/2}} dx$$

Optimal (type 3, 70 leaves, 6 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a + b \text{Tanh}[x]^2}}{\sqrt{a - b}}\right]}{(a + b)^{5/2}} - \frac{1}{3 (a + b) (a + b \text{Tanh}[x]^2)^{3/2}} - \frac{1}{(a + b)^2 \sqrt{a + b \text{Tanh}[x]^2}}$$

Result (type 3, 359 leaves):

$$\begin{aligned} & \sqrt{\frac{a - b + a \operatorname{Cosh}[2x] + b \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \left(-\frac{4}{3(a+b)^3} - \right. \\ & \left. \frac{4b^2}{3(a+b)^3(a-b+a\operatorname{Cosh}[2x]+b\operatorname{Cosh}[2x])^2} - \frac{10b}{3(a+b)^3(a-b+a\operatorname{Cosh}[2x]+b\operatorname{Cosh}[2x])} \right) + \\ & \left((1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2x]}{(1 + \operatorname{Cosh}[x])^2}} \sqrt{\frac{a - b + (a+b)\operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \left(\operatorname{Log}\left[-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] - \right. \right. \\ & \left. \left. \operatorname{Log}\left[a + b + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a+b} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) \right. \\ & \left. (-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right) \sqrt{\frac{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2)^2}} \right) / \\ & \left((a+b)^{5/2} \sqrt{a - b + (a+b)\operatorname{Cosh}[2x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) \end{aligned}$$

Problem 253: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Coth}[x]}{(a + b \operatorname{Tanh}[x]^2)^{5/2}} dx$$

Optimal (type 3, 108 leaves, 9 steps):

$$\begin{aligned} & -\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a}}\right]}{a^{5/2}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tanh}[x]^2}}{\sqrt{a+b}}\right]}{(a+b)^{5/2}} + \\ & \frac{b}{3a(a+b)(a+b \operatorname{Tanh}[x]^2)^{3/2}} + \frac{b(2a+b)}{a^2(a+b)^2 \sqrt{a+b \operatorname{Tanh}[x]^2}} \end{aligned}$$

Result (type 3, 966 leaves):

$$\begin{aligned} & \sqrt{\frac{a - b + a \operatorname{Cosh}[2x] + b \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \left(\frac{b(7a+3b)}{3a^2(a+b)^3} + \frac{4b^3}{3a(a+b)^3(a-b+a\operatorname{Cosh}[2x]+b\operatorname{Cosh}[2x])^2} + \right. \\ & \left. \frac{2b^2(8a+3b)}{3a^2(a+b)^3(a-b+a\operatorname{Cosh}[2x]+b\operatorname{Cosh}[2x])} \right) + \\ & \frac{1}{2a^2(a+b)^2} \left((3a^2 + 8ab + 4b^2) (1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2x]}{(1 + \operatorname{Cosh}[x])^2}} \sqrt{\frac{a - b + (a+b)\operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \right) \end{aligned}$$

$$\begin{aligned}
 & \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \operatorname{Log}\left[a + 2b + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] + \right. \\
 & \quad \left. \operatorname{Log}\left[a + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + 2b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) \\
 & \quad \left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2 \right) \sqrt{\frac{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) / \\
 & \quad \left(4\sqrt{a} \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) + \\
 & \quad \frac{1}{\sqrt{a-b+(a+b) \operatorname{Cosh}[2x]}} 3a^2 \sqrt{1 + \operatorname{Cosh}[2x]} \sqrt{\frac{a-b+(a+b) \operatorname{Cosh}[2x]}{1 + \operatorname{Cosh}[2x]}} \\
 & \quad \left(\left(4 \operatorname{Cosh}[x]^2 \sqrt{-2b+a(1+\operatorname{Cosh}[2x]) + b(1+\operatorname{Cosh}[2x])} \operatorname{Coth}[x] \right. \right. \\
 & \quad \left. \left(-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{1+\operatorname{Cosh}[2x]}}{\sqrt{b(-1+\operatorname{Cosh}[2x]) + a(1+\operatorname{Cosh}[2x])}}\right]}{\sqrt{a}} + \frac{1}{\sqrt{a+b}} \operatorname{Log}\left[a \sqrt{1 + \operatorname{Cosh}[2x]} + b \right. \right. \\
 & \quad \left. \left. \sqrt{1 + \operatorname{Cosh}[2x]} + \sqrt{a+b} \sqrt{b(-1 + \operatorname{Cosh}[2x]) + a(1 + \operatorname{Cosh}[2x])} \right] \right) \right) \\
 & \quad \left. \operatorname{Sinh}[2x] \right) / \left(3(1 + \operatorname{Cosh}[2x])^2 \sqrt{a-b+(a+b) \operatorname{Cosh}[2x]} \right) - \\
 & \quad \left((1 + \operatorname{Cosh}[x]) \sqrt{\frac{1 + \operatorname{Cosh}[2x]}{(1 + \operatorname{Cosh}[x])^2}} \left(-\operatorname{Log}\left[\operatorname{Tanh}\left[\frac{x}{2}\right]^2\right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[a + 2b + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[a + a \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + 2b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + \sqrt{a} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}\right] \right) \right)
 \end{aligned}$$

$$\left((-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2) \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right) \sqrt{\frac{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}{\left(-1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2}} \right) / \right. \\ \left. \left(4 \sqrt{a} \sqrt{1 + \operatorname{Cosh}[2x]} \sqrt{\left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \sqrt{4b \operatorname{Tanh}\left[\frac{x}{2}\right]^2 + a \left(1 + \operatorname{Tanh}\left[\frac{x}{2}\right]^2\right)^2} \right) \right)$$

Problem 254: Result unnecessarily involves higher level functions.

$$\int \frac{\operatorname{Coth}[x]^2}{(a + b \operatorname{Tanh}[x]^2)^{5/2}} dx$$

Optimal (type 3, 131 leaves, 7 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^2}}\right]}{(a+b)^{5/2}} + \frac{b \operatorname{Coth}[x]}{3a(a+b)(a+b \operatorname{Tanh}[x]^2)^{3/2}} + \\ \frac{b(7a+4b) \operatorname{Coth}[x]}{3a^2(a+b)^2 \sqrt{a+b \operatorname{Tanh}[x]^2}} - \frac{(3a+2b)(a+4b) \operatorname{Coth}[x] \sqrt{a+b \operatorname{Tanh}[x]^2}}{3a^3(a+b)^2}$$

Result (type 4, 246 leaves):

$$\frac{1}{3 \sqrt{2} a^3 (a+b)^3} \sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sech}[x]^2}$$

$$\left(\left(\left(3 \sqrt{2} a^3 \operatorname{Coth}[x] \left((a+b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{CsCh}[x]^2}}{b}}\right], 1\right] - \right. \right. \right.$$

$$\left. \left. \left. a \operatorname{EllipticPi}\left[\frac{b}{a+b}, \operatorname{ArcSin}\left[\frac{\sqrt{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{CsCh}[x]^2}}{b}}\right], 1\right] \right) \right) \right) /$$

$$\left(b \sqrt{\frac{(a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{CsCh}[x]^2}{b}} \right) -$$

$$\left((a+b) \left(3 (a+b)^2 (a-b+(a+b) \operatorname{Cosh}[2x])^2 \operatorname{Coth}[x] + 2 a b^3 \operatorname{Sinh}[2x] + \right. \right.$$

$$\left. \left. b^2 (9 a + 5 b) (a-b+(a+b) \operatorname{Cosh}[2x]) \operatorname{Sinh}[2x] \right) \right) / (a-b+(a+b) \operatorname{Cosh}[2x])^2 \right)$$

Problem 259: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Tanh}[x] (a+b \operatorname{Tanh}[x]^4)^{3/2} dx$$

Optimal (type 3, 124 leaves, 9 steps):

$$-\frac{1}{4} \sqrt{b} (3a+2b) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Tanh}[x]^2}{\sqrt{a+b \operatorname{Tanh}[x]^4}}\right] + \frac{1}{2} (a+b)^{3/2} \operatorname{ArcTanh}\left[\frac{a+b \operatorname{Tanh}[x]^2}{\sqrt{a+b} \sqrt{a+b \operatorname{Tanh}[x]^4}}\right] -$$

$$\frac{1}{4} (2(a+b) + b \operatorname{Tanh}[x]^2) \sqrt{a+b \operatorname{Tanh}[x]^4} - \frac{1}{6} (a+b \operatorname{Tanh}[x]^4)^{3/2}$$

Result (type 3, 62021 leaves): Display of huge result suppressed!

Problem 260: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Tanh}[x] \sqrt{a+b \operatorname{Tanh}[x]^4} dx$$

Optimal (type 3, 89 leaves, 8 steps):

$$-\frac{1}{2} \sqrt{b} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \operatorname{Tanh}[x]^2}{\sqrt{a+b \operatorname{Tanh}[x]^4}}\right] + \frac{1}{2} \sqrt{a+b} \operatorname{ArcTanh}\left[\frac{a+b \operatorname{Tanh}[x]^2}{\sqrt{a+b} \sqrt{a+b \operatorname{Tanh}[x]^4}}\right] - \frac{1}{2} \sqrt{a+b \operatorname{Tanh}[x]^4}$$

Result (type 3, 31 650 leaves): Display of huge result suppressed!

Problem 261: Unable to integrate problem.

$$\int \frac{\operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^4}} dx$$

Optimal (type 3, 40 leaves, 4 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{a+b \operatorname{Tanh}[x]^2}{\sqrt{a+b} \sqrt{a+b \operatorname{Tanh}[x]^4}}\right]}{2 \sqrt{a+b}}$$

Result (type 8, 17 leaves):

$$\int \frac{\operatorname{Tanh}[x]}{\sqrt{a+b \operatorname{Tanh}[x]^4}} dx$$

Problem 262: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tanh}[x]}{(a+b \operatorname{Tanh}[x]^4)^{3/2}} dx$$

Optimal (type 3, 74 leaves, 6 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{a+b \operatorname{Tanh}[x]^2}{\sqrt{a+b} \sqrt{a+b \operatorname{Tanh}[x]^4}}\right]}{2 (a+b)^{3/2}} - \frac{a-b \operatorname{Tanh}[x]^2}{2 a (a+b) \sqrt{a+b \operatorname{Tanh}[x]^4}}$$

Result (type 3, 33271 leaves): Display of huge result suppressed!

Problem 263: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Tanh}[x]}{(a+b \operatorname{Tanh}[x]^4)^{5/2}} dx$$

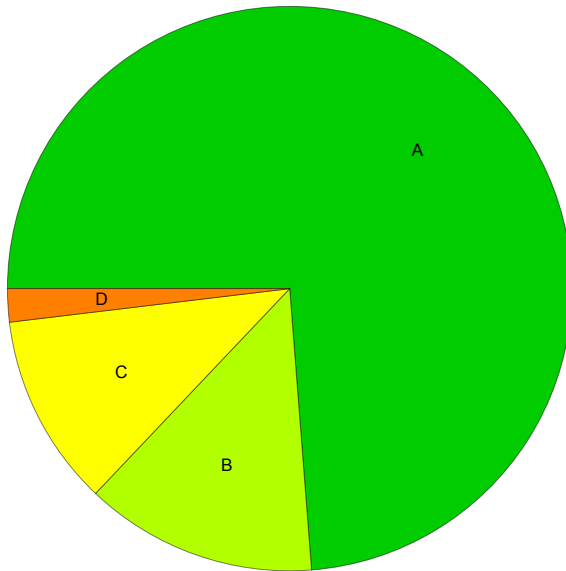
Optimal (type 3, 118 leaves, 7 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{a+b \operatorname{Tanh}[x]^2}{\sqrt{a+b} \sqrt{a+b \operatorname{Tanh}[x]^4}}\right]}{2 (a+b)^{5/2}} - \frac{a-b \operatorname{Tanh}[x]^2}{6 a (a+b) (a+b \operatorname{Tanh}[x]^4)^{3/2}} - \frac{3 a^2 - b (5 a + 2 b) \operatorname{Tanh}[x]^2}{6 a^2 (a+b)^2 \sqrt{a+b \operatorname{Tanh}[x]^4}}$$

Result (type 3, 41 215 leaves): Display of huge result suppressed!

Summary of Integration Test Results

263 integration problems



A - 194 optimal antiderivatives

B - 35 more than twice size of optimal antiderivatives

C - 29 unnecessarily complex antiderivatives

D - 5 unable to integrate problems

E - 0 integration timeouts